

Crystal Growth: Physics, Technology and Modeling

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Lecture 8. Liquid phase epitaxy and lateral overgrowth

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<http://www.unipress.waw.pl/~stach/cg-2022-23>

Liquid phase epitaxy and lateral overgrowth

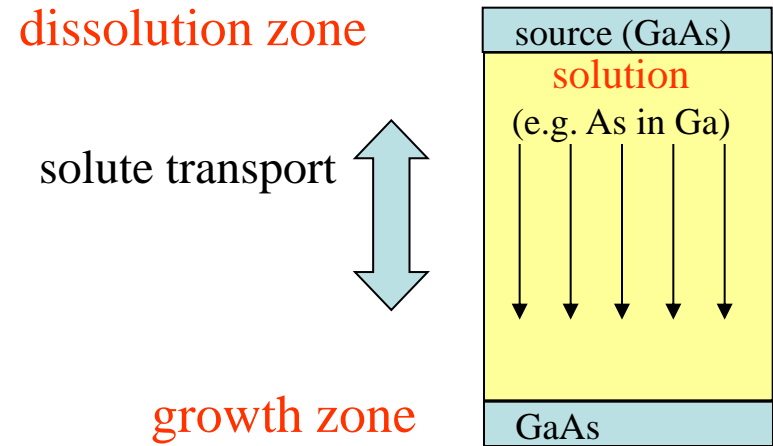
Outline:

- **definition + idea of LPE**
- **history and technical aspects**
- **solute transport during LPE growth; diffusion, convection**
- **Liquid Phase Electroepitaxy**

- **Epitaxial Lateral Overgrowth**
- **principle and growth control**
- **filtration of dislocations in ELO**
- **strain in ELO structures**

Liquid Phase Epitaxy - LPE

technique of epitaxial thin films growth *from metallic solution*



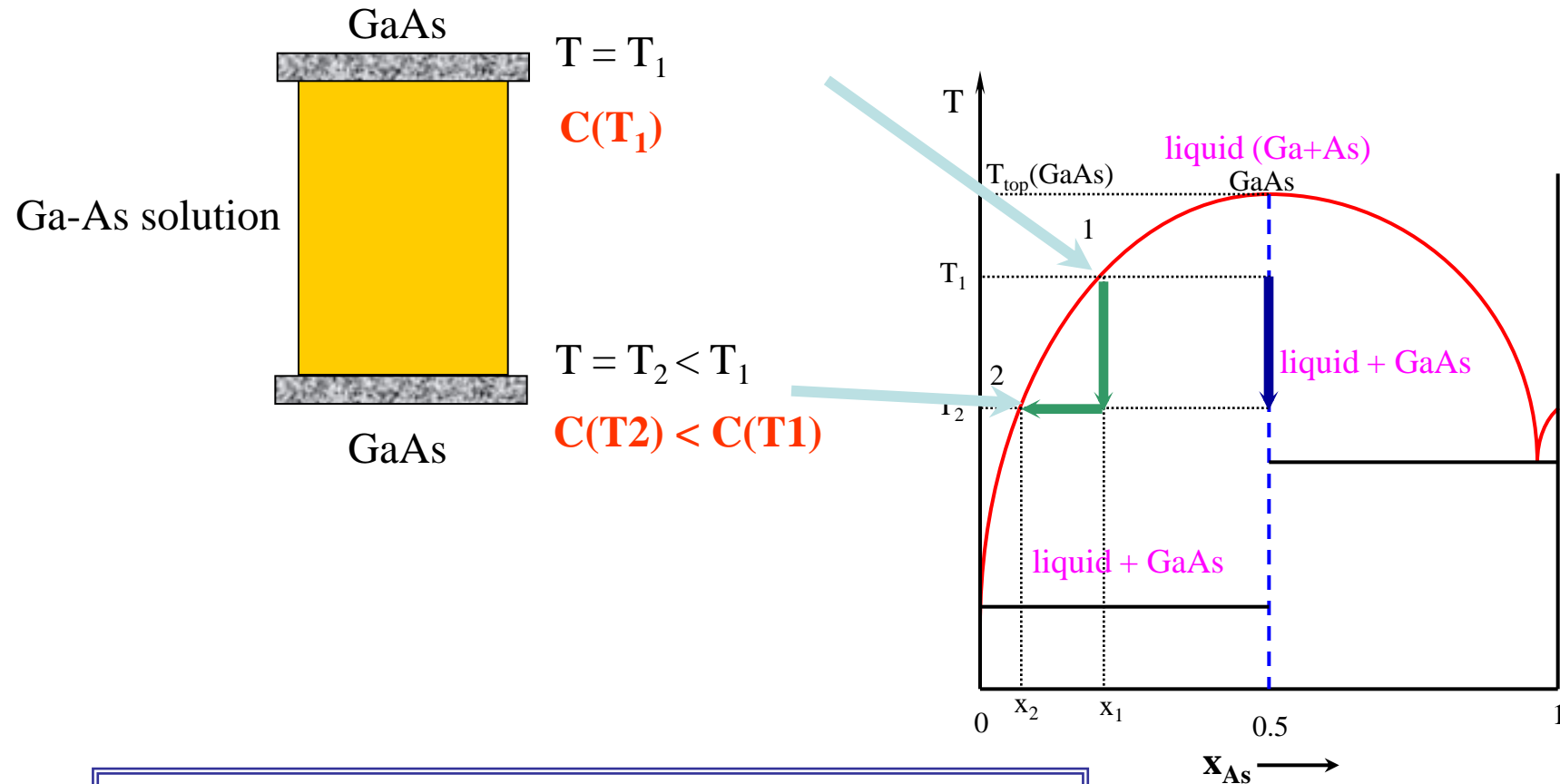
advantages of solution growth & epitaxy

properties of solvent required:

- crystal component (e.g. Ga for GaAs)
or low solubility in the crystal (Bi, Sn, In, Pb, etc.)
- low melting point
- high solubility of solute @ T_{epi}
- low vapor pressure @ T_{epi}
- high chemical stability
- high purity
- low price ???

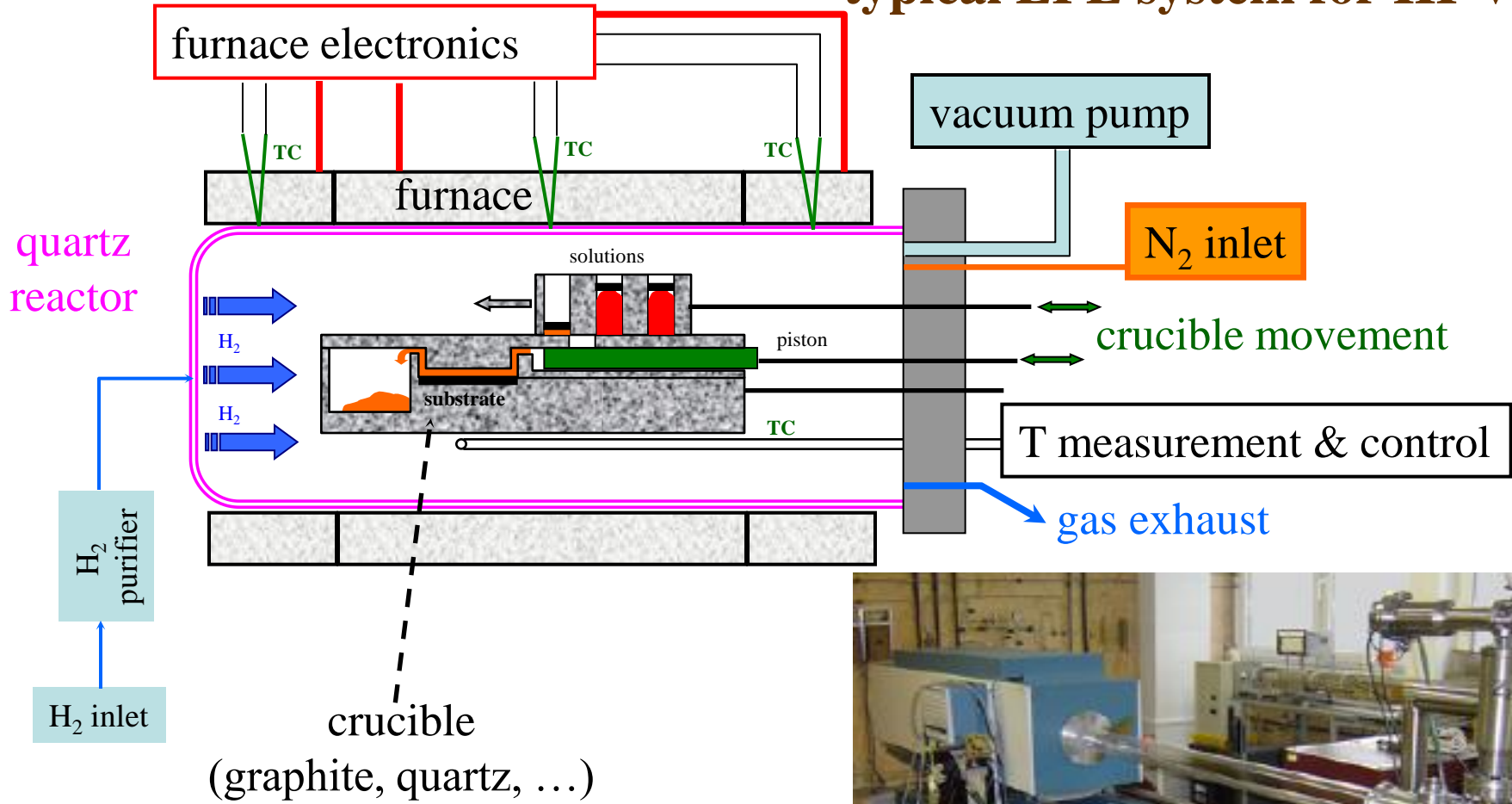
Idea of LPE (example: homoepitaxy of GaAs on GaAs substrate)

growth in T gradient



LPE – equilibrium growth method !!!

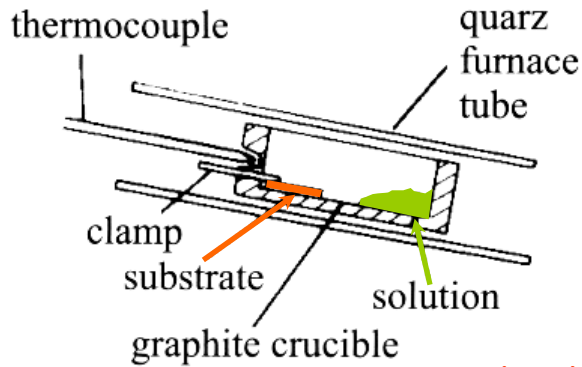
typical LPE system for III-V's



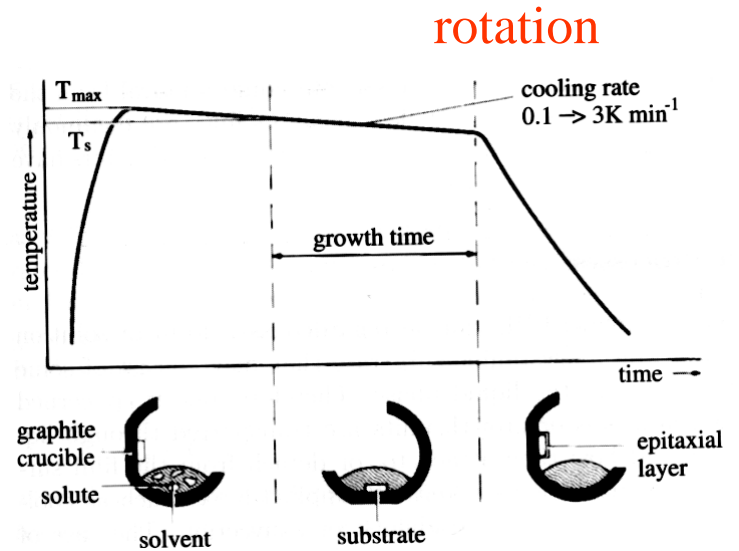
horizontal system
ITE Warszawa



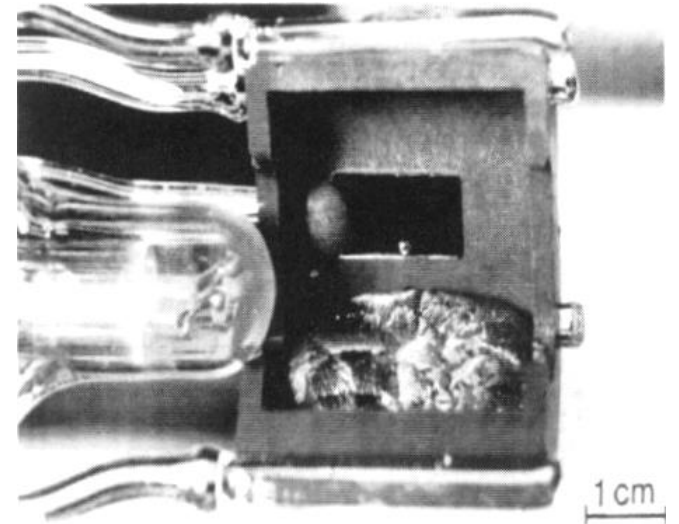
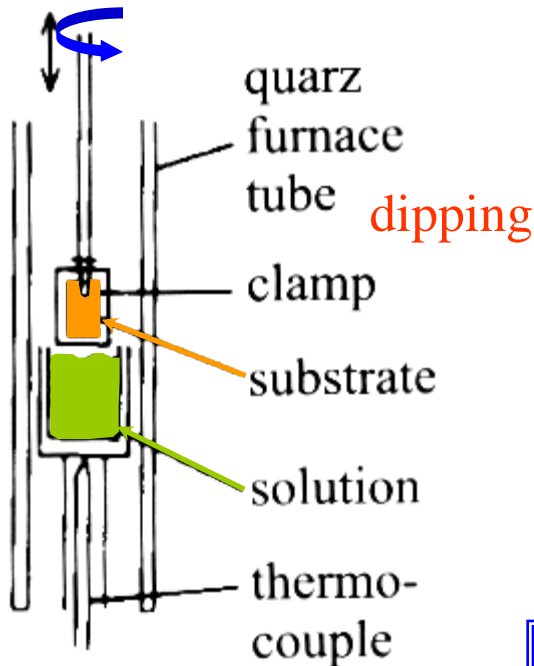
Crucibles in LPE



tipping

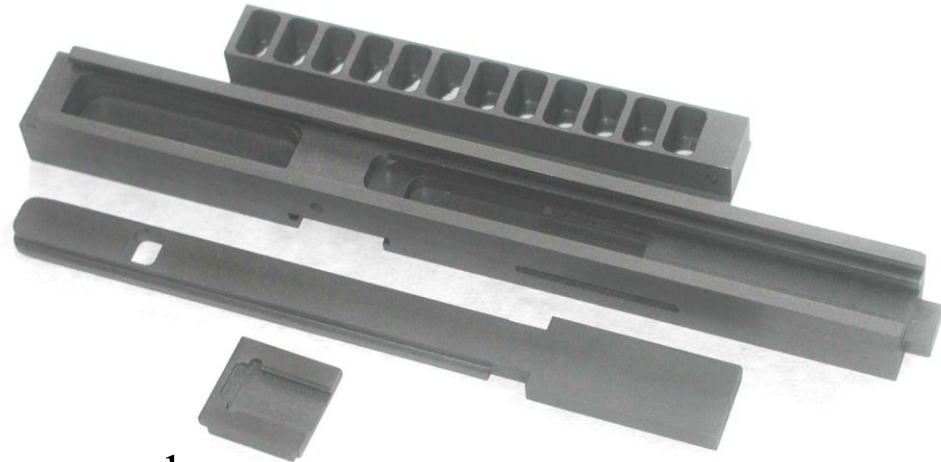
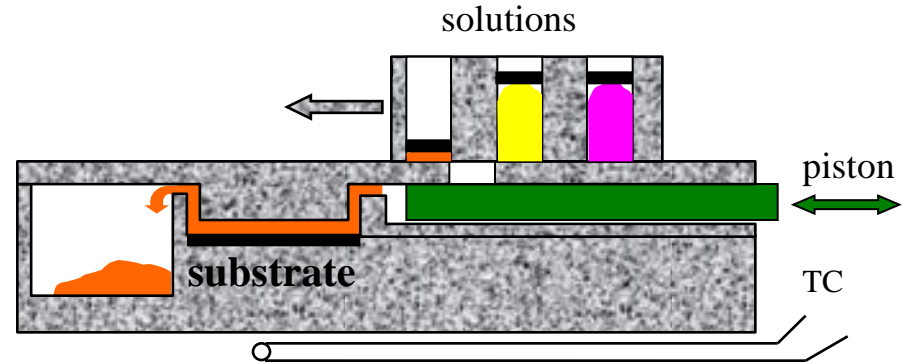
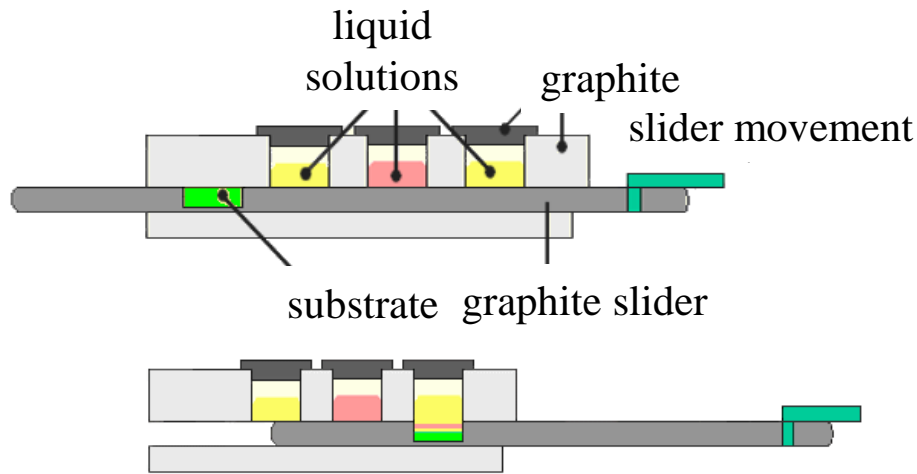


rotation



growth of single layers

Crucibles in LPE cont.



IF PAN

advantages:

- growth of multilayer structures
- thin layer of the solution
- „skin” of oxides on the solution surface removed

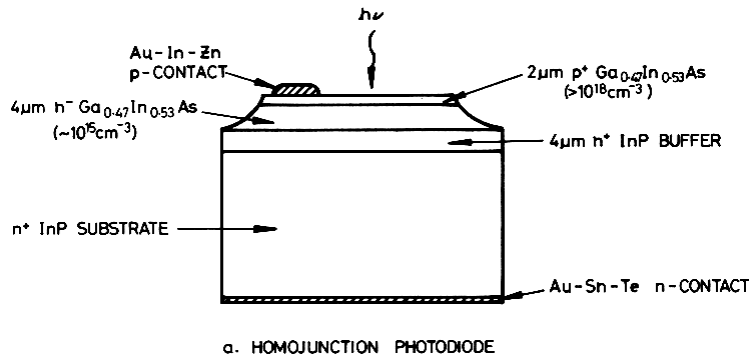
disadvantages:

- blurred (not sharp) interfaces

History

H. Nelson: *Epitaxial growth from the liquid state and its application to the fabrication of tunnel and laser diodes*
 RCA Rev. 24 (1963) 603.

Nobel 2000 - H. Kroemer, J. Kilby, Z. Alfierow
 “for developing semiconductor heterostructures used in high-speed- and opto-electronics”



Why LPE:

- „cheap and easy”
- high purity of layers (impurity segregation)
- selective area growth easy
- broad range of compounds can be grown (As, P, ...)
- „safe” method (as compared to MOVPE)

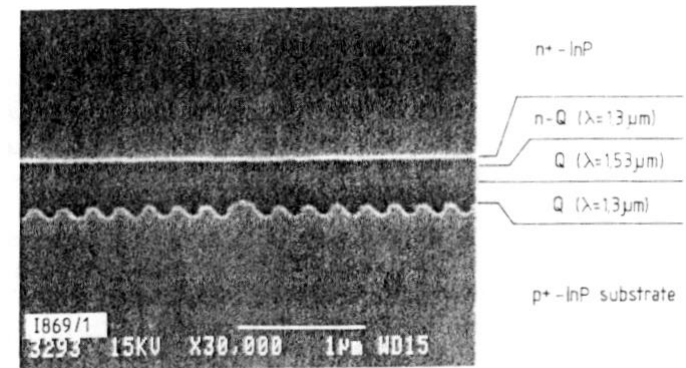
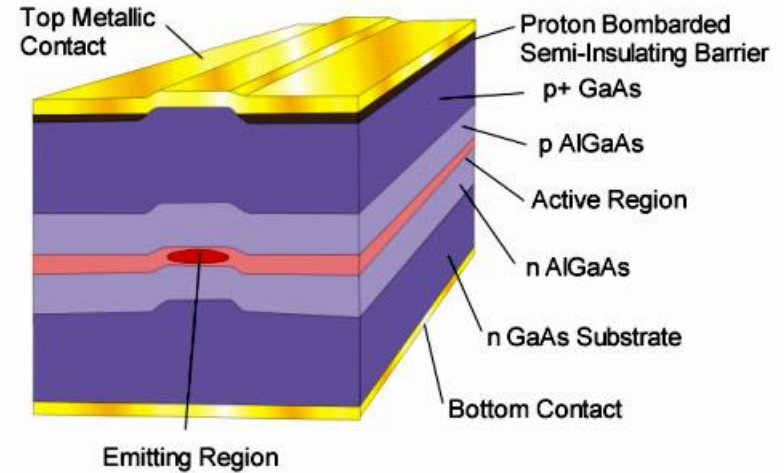
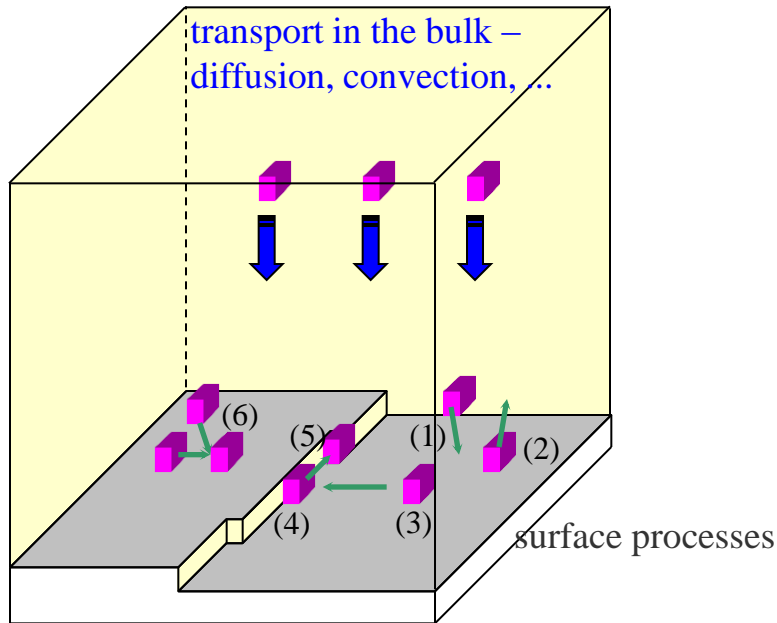


Fig. 14. InGaAsP DFB laser structure grown nearly dissolution-free over a first order grating, after [70]. For details, see text

Growth kinetics



transport of solute in the bulk of solution



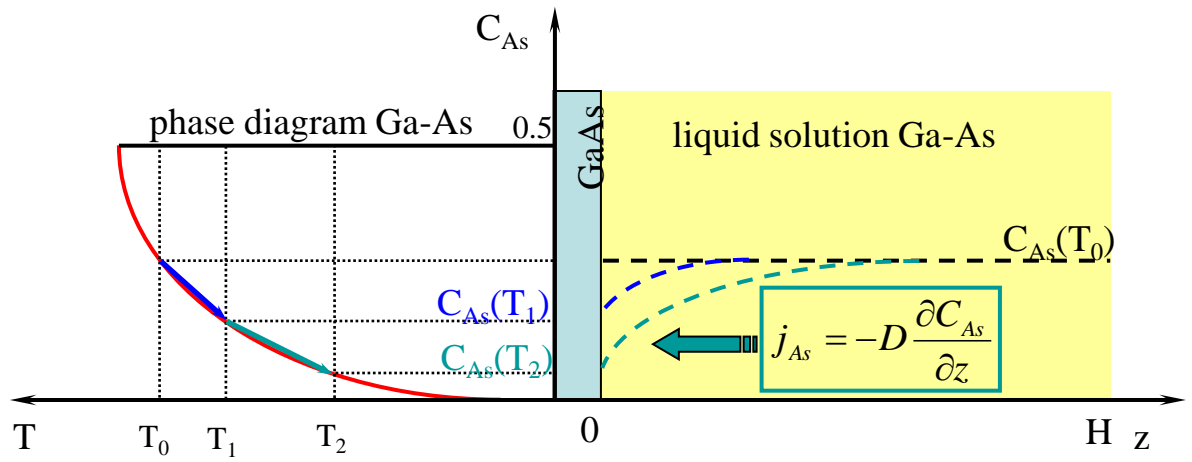
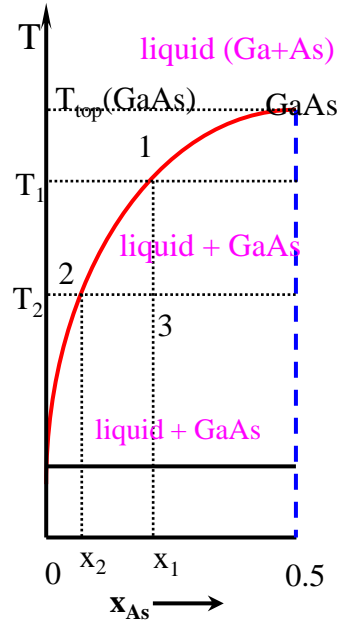
surface processes

the slower one determines the growth rate

usually

the growth temperature in LPE is so high (surface processes so fast), while the bulk solute transport is slow, that solute transport in the bulk of the solution determines the growth rate

LPE: diffusion controlled growth – example: GaAs growth from Ga-As solution



assumptions:

- fast surface kinetics
- no convective mixing
- low growth rate V_{gr}
- fast heat transport
- no diffusion in solid state

transport:

mass

heat

~~$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2} + V_{gr} \frac{\partial C}{\partial z}$$~~

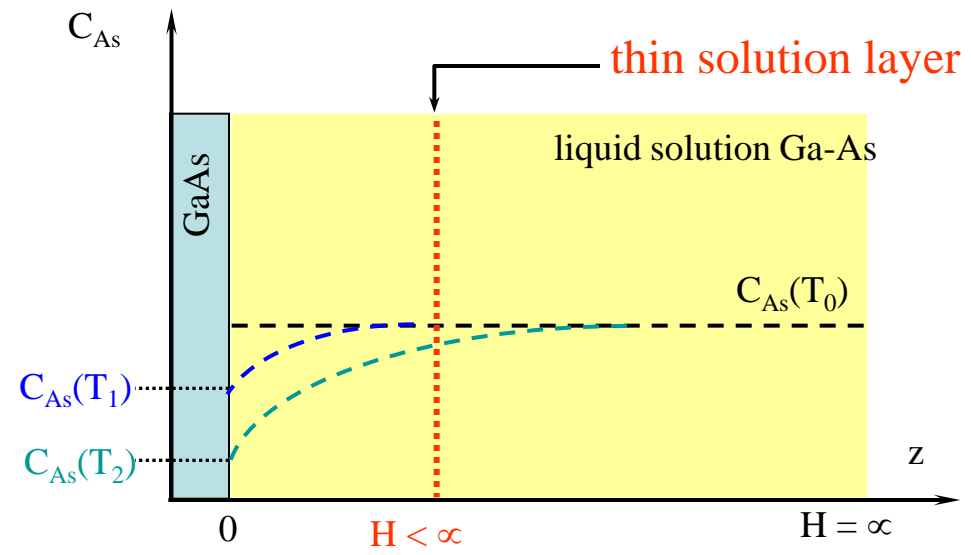
~~$$\frac{\partial T}{\partial t} = k \frac{\partial^2 T}{\partial z^2} + V_{gr} \frac{\partial T}{\partial z}$$~~

mass flux continuity condition

~~$$V_{gr} (C_{s,z=0} - C_{l,z=0}) = D_l \frac{\partial C_l}{\partial z} \Big|_{(z=0)} - D_s \frac{\partial C_s}{\partial z} \Big|_{(z=0)}$$~~

**+ initial and boundary conditions
(which depend on LPE version, e.g. T(t))**

LPE: diffusion controlled growth – example: GaAs growth from Ga-As solution



equations

$$\frac{\partial C}{\partial t} = D \frac{\partial^2 C}{\partial z^2}$$

$$V_{gr} (C_{s,z=0} - C_{l,z=0}) = D_l \frac{\partial C_l}{\partial z} \Big|_{(z=0)}$$

infinite solution

$$H = \infty \iff H \gg \sqrt{D_l t}$$

Ga - As: $T = 800^\circ C$ $D_l \approx 4 \cdot 10^{-5} \text{ cm}^2/\text{s}$
 $t = 30 \text{ min}$ $\sqrt{D_l t} = 2.6 \text{ mm}$

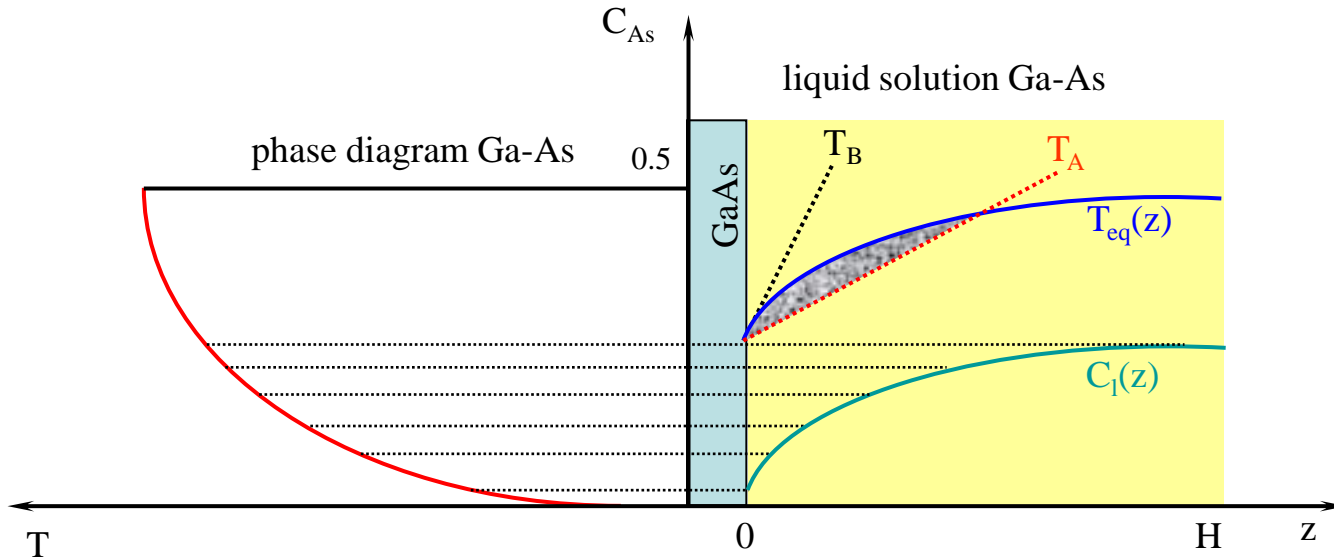
initial and boundary conditions

$$C_l(z=0, t) = C_{eq}(T(t))$$

$$\frac{\partial C_l}{\partial z} (z \rightarrow \infty, t) = 0$$

equilibrium at the solid/liquid interface LPE version

LPE: constitutional supersaturation



Udayashankar et al., *Bull. Mater. Sci* 26 (2003) 685

theory:

increase grad T at the interface
(T_B instead of T_A)

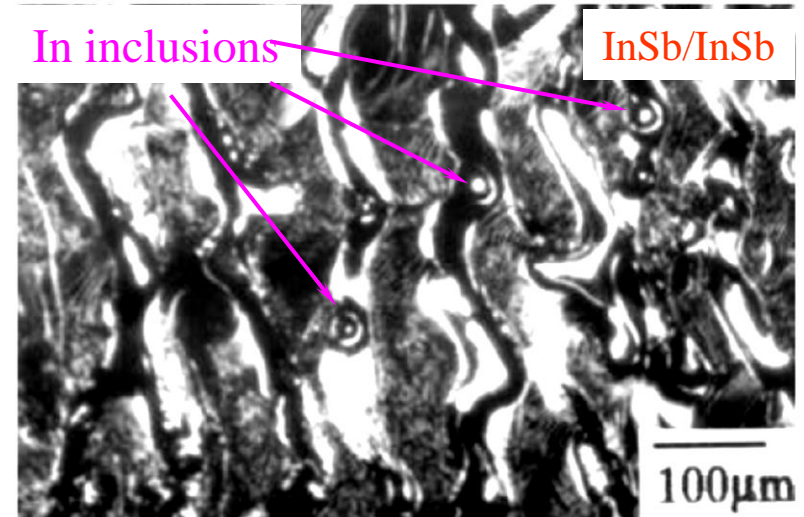
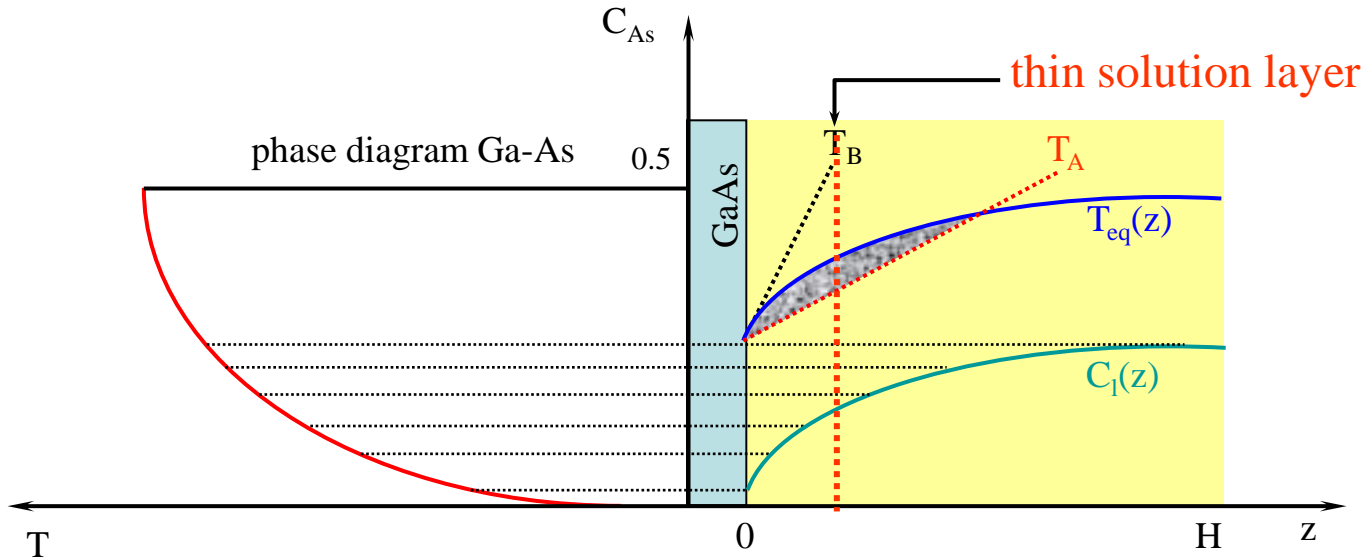


Figure 3. Film showing various surface features like ridges, valleys, inclusions, etc.

LPE: constitutional supersaturation



Udayashankar et al., Bull. Mater. Sci 26 (2003) 685

theory:

increase grad T at the interface
(T_B instead of T_A)

practice:

- decrease concentration gradient
- thinner solution layer
- lower the growth rate

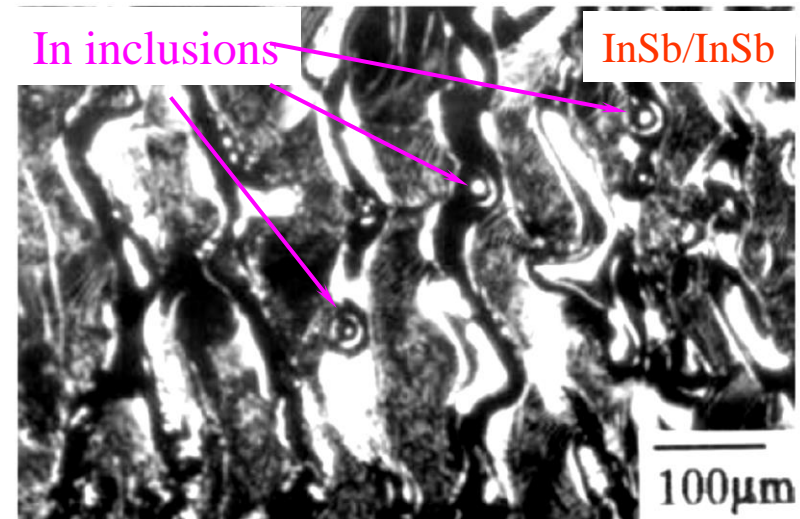


Figure 3. Film showing various surface features like ridges, valleys, inclusions, etc.

LPE: natural convection

natural convection

$$\rho = \rho(T, C) + \text{gravity}$$

convection **thermal** solutal

$$\frac{\partial \rho}{\partial T} < 0$$

$$\frac{\partial \rho}{\partial C} ???$$

assumptions:

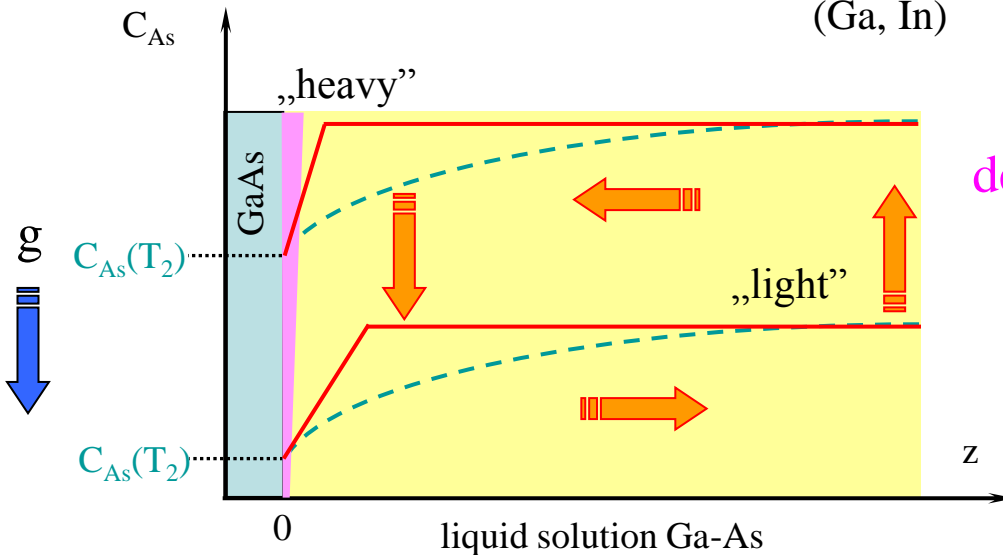
- no external mixing
- vertical substrate
- $T(x, y, z) = \text{const.}$
solutal convection only

typical III-V solutions

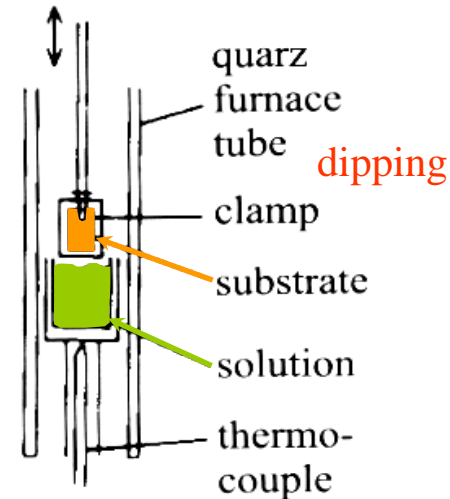
$$\rho_{\text{solvent}} > \rho_{\text{solute}}$$

(Ga, In) (As, P)

$$\frac{\partial \rho}{\partial C} < 0$$

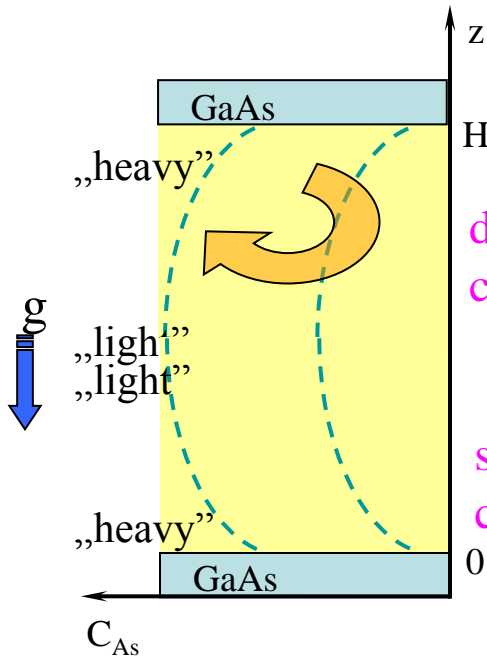


destabilizing solute distribution (As)
epilayer thickness gradient



LPE: natural convection cont.

S. Krukowski's lecture



destabilizing solute (As)
concentration distribution

stabilizing solute (As)
concentration distribution

if the Rayleigh's number is low $Ra < 1000$



diffusion dominates

usually both $gradT$ and $gradC$ exist

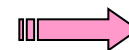
$$Ra_C = g \cdot \Delta C \cdot \beta \cdot H^3 / D\nu < 1000$$

$$Ra_T = g \cdot \Delta T \cdot \alpha \cdot H^3 / \kappa\nu < 1000$$



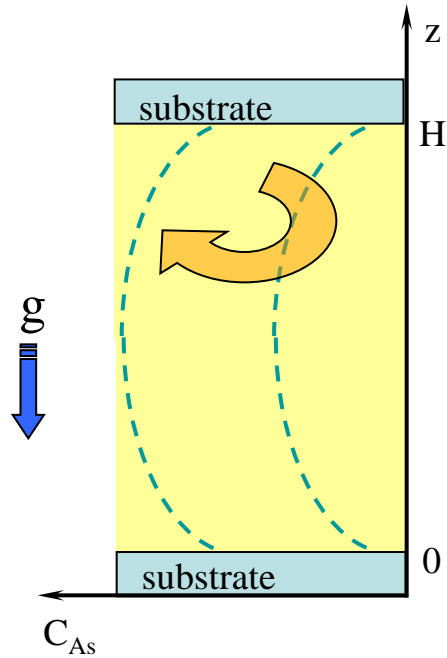
- $\kappa \gg D$ – small ΔC leads to convective flow
- solutal convection \gg thermal convection
- $Ra \sim H^3$ - solution layer thickness !!!

Tiller JCG 2 (1968) 69: no thermal convection if $H < 5$ mm
no solutal convection if $H < 2$ mm

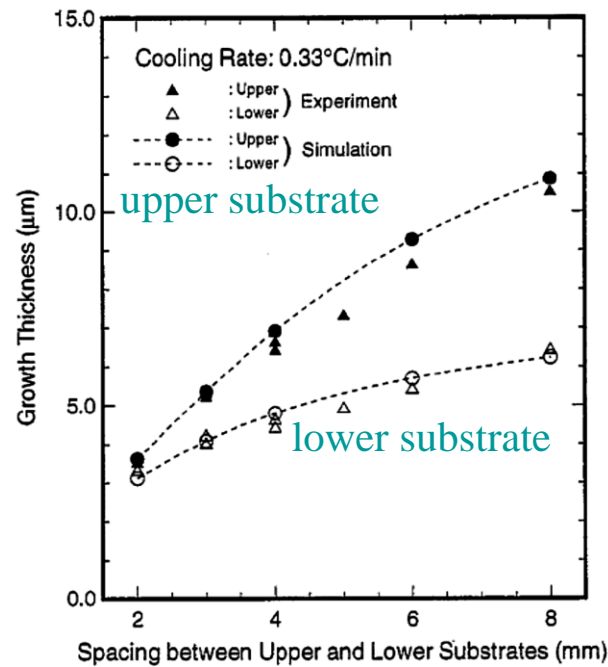


LPE from thin solution layer !!!

LPE: natural convection cont.



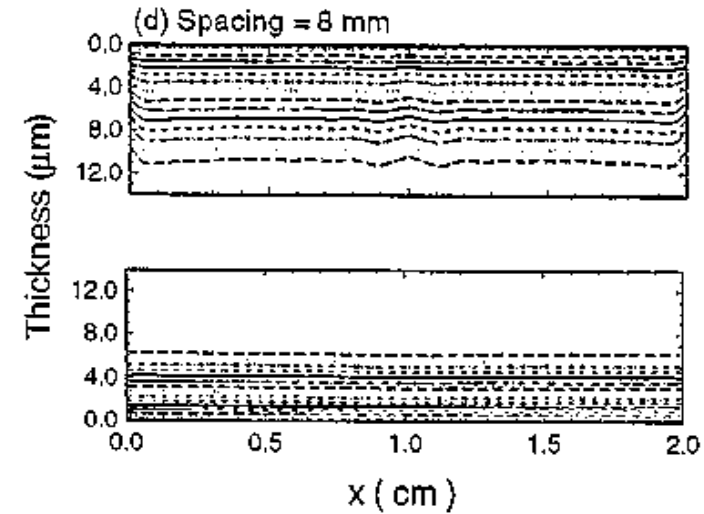
Kimura et al. JCG 167 (1996) 516



for thin solutions growth on both substrates similar

LPE of Si from Sn solution

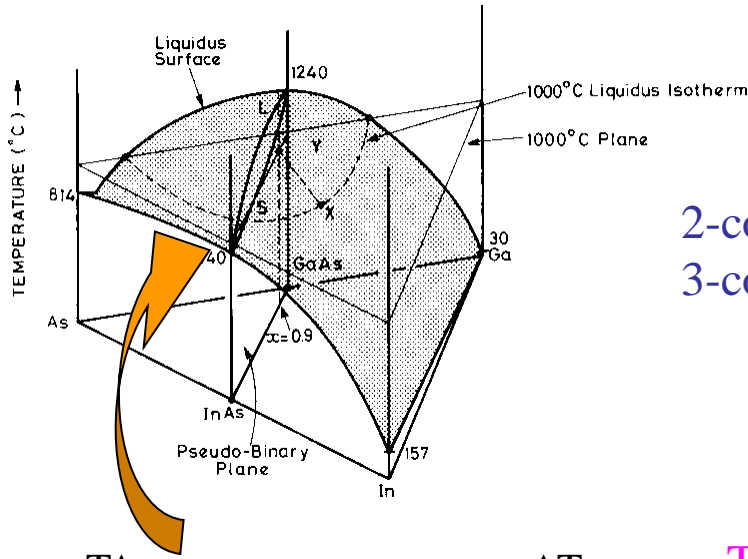
simulation + exp.



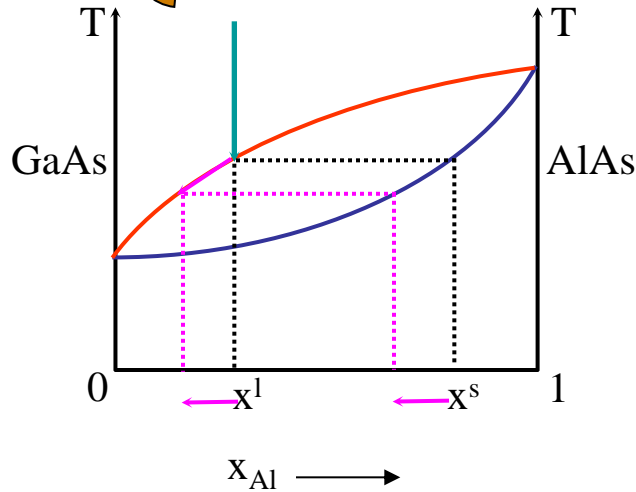
LPE of multicomponent systems (example: GaAlAs on GaAs)

the Gibbs phase rule: $f(\text{degrees of freedom}) = C(\text{components}) - p(\text{phases}) + 2(p; T)$

e.g. Ga-Al-As \Leftrightarrow $\text{Ga}_{1-x}\text{Al}_x\text{As}$ 3 2 $p = \text{const.} \Rightarrow f = 2 (T, x)$

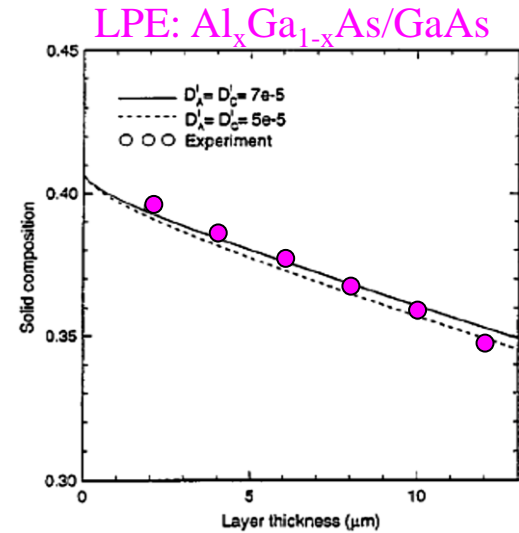


2-component system: composition of epilayer fixed
 3-component system: composition of epilayer (x) - variable



$T \downarrow - \text{grad } x^s$

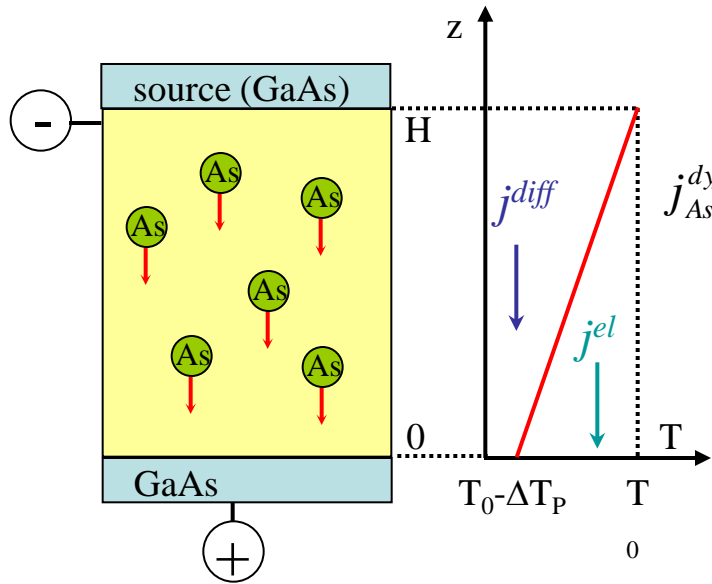
$T = \text{const.}$
 \downarrow
 $x^s = \text{const.}$



LPE growth of compositionally uniform AlGaAs layers challenging

Liquid phase electroepitaxy (LPEE)

$T_0 = \text{const.}$ + DC current flow through the solid/liquid interface



Peltier effect

$$j_{As}^{dyf} = D \cdot \frac{C(T_0) - C(T_0 - \Delta T_P)}{H}$$

$$= D \cdot \frac{dC}{dT} \cdot \frac{\Delta T_P}{H}$$

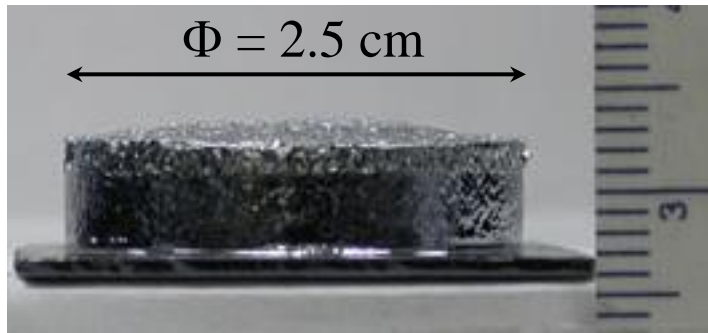
electrotransport

„electron wind” effect

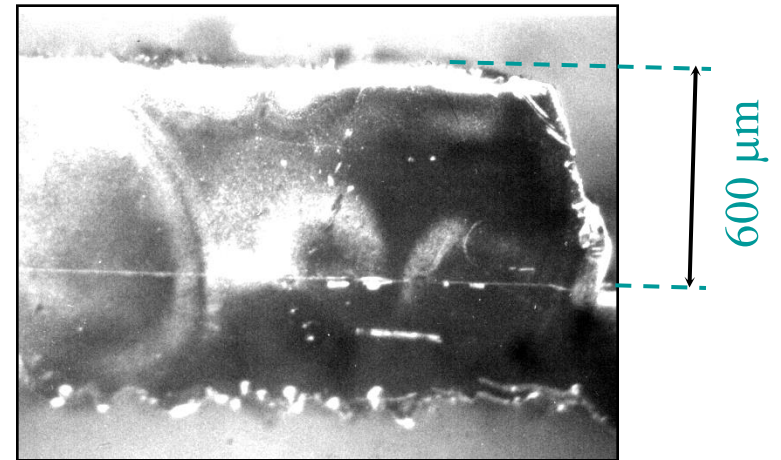
$$j_{As}^{el} = \mu \cdot E \cdot C(T_0)$$

$$= \mu \cdot \sigma \cdot j_e \cdot C(T_0)$$

$V_{gr} \propto \text{electric current density}$



LPEE InGaAs/GaAs

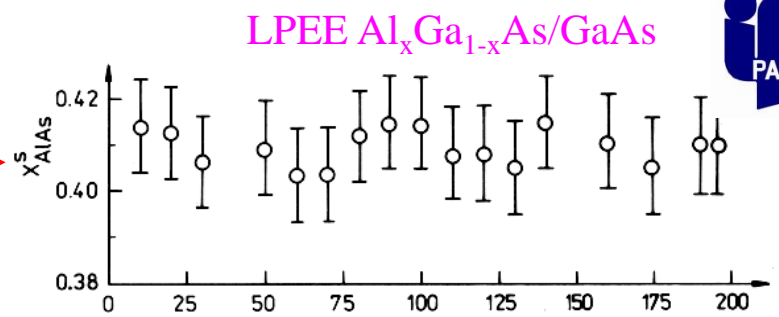


LPEE AlGaSb/GaSb

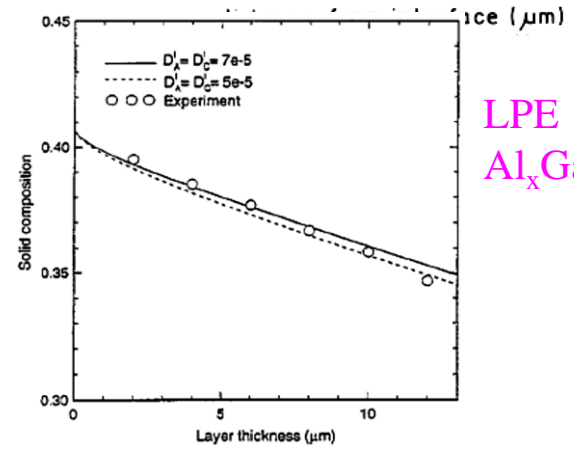
LPEE - advantages

- compositional uniformity
- *in situ* monitoring
- time markers
- simultaneous growth of many crystals
- „easier” V_{gr} control
- surface stability

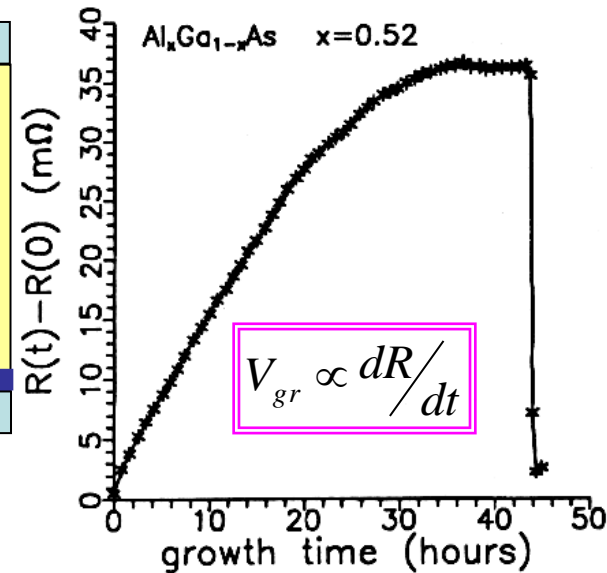
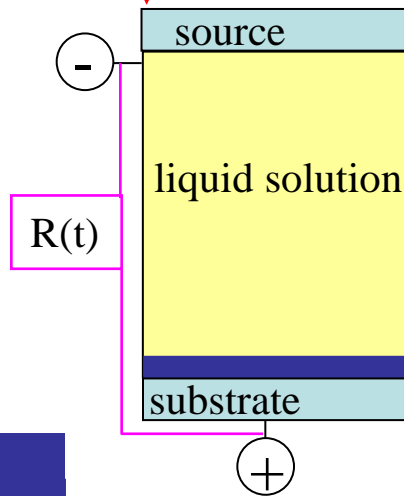
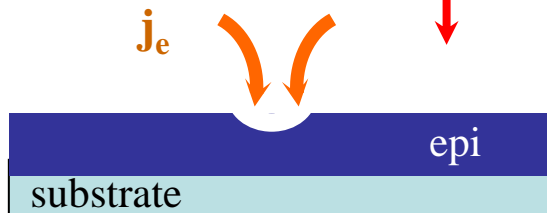
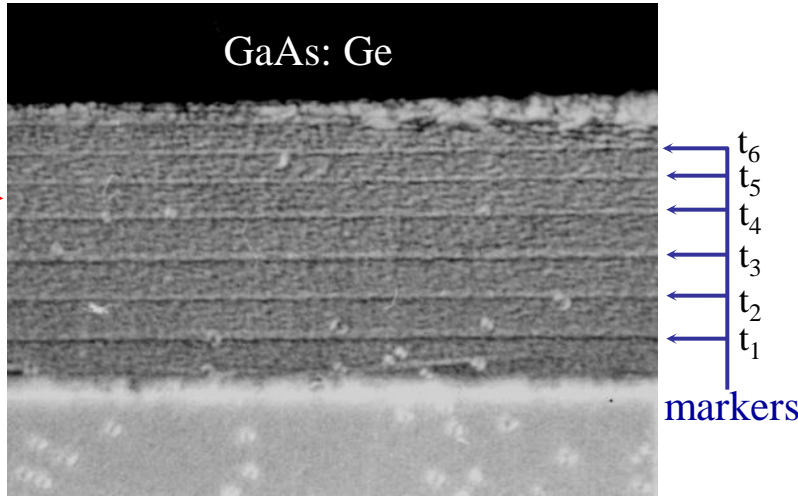
$T = \text{const.}$



~ current density

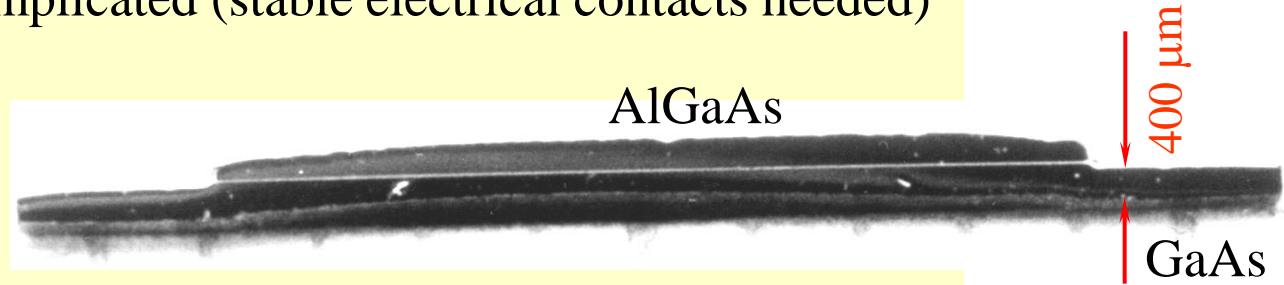


LPE $\text{Al}_x\text{Ga}_{1-x}\text{As}/\text{GaAs}$



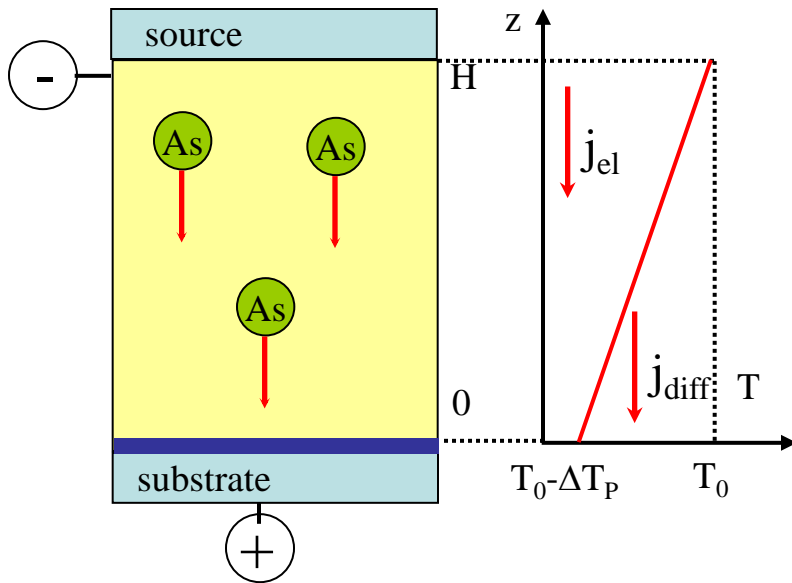
LPEE - disadvantages

- LPEE system more complicated (stable electrical contacts needed)

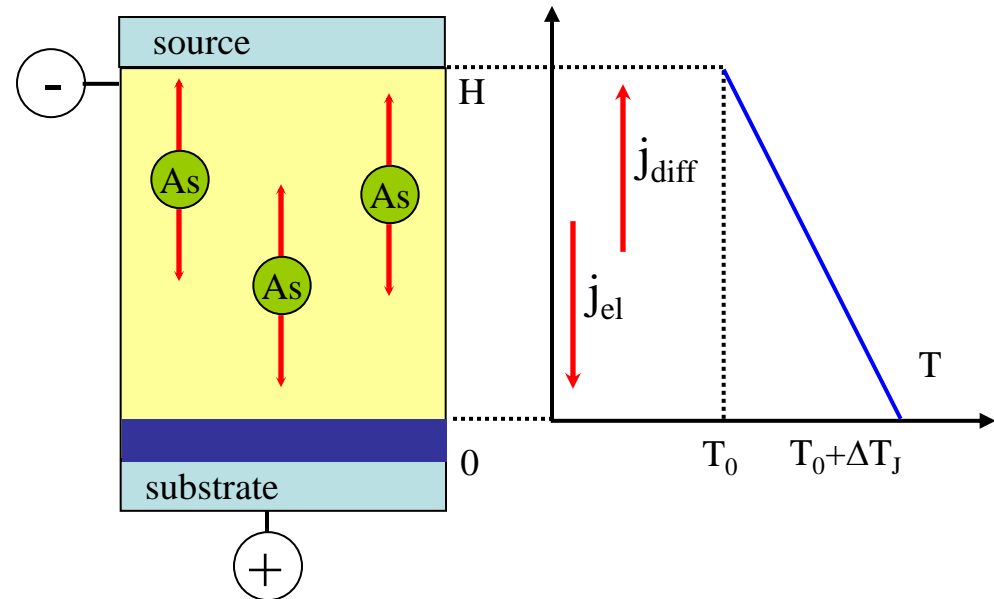


- Joule effect limiting the crystal thickness

no Joule effect



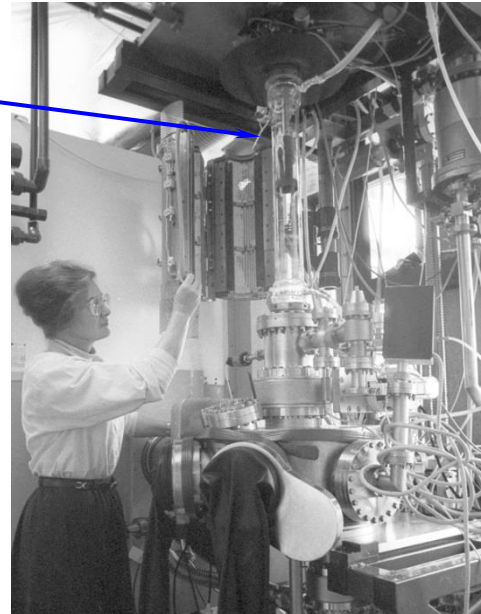
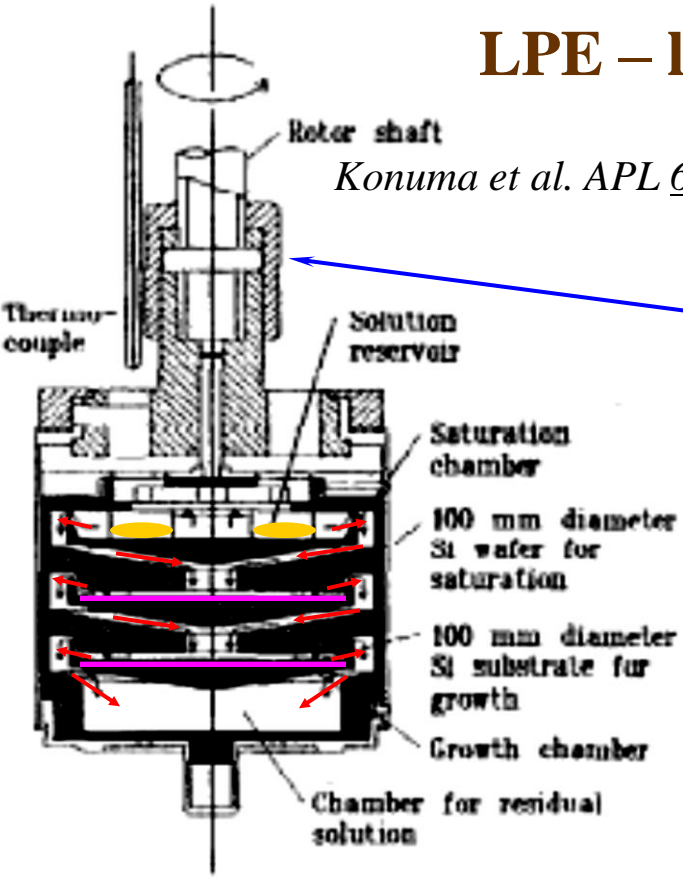
with Joule effect



growth can be continued if $j_{el} \downarrow$

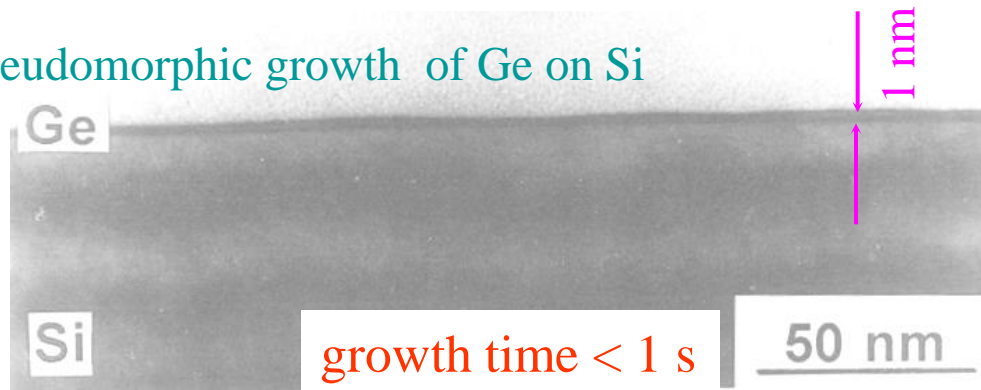
LPE – low dimensional structures

Konuma et al. APL 63 (1993) 205



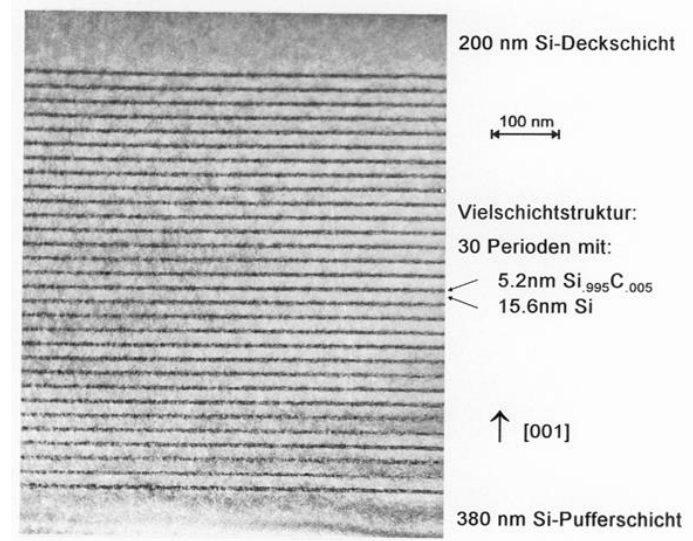
4" substrate !!!

pseudomorphic growth of Ge on Si

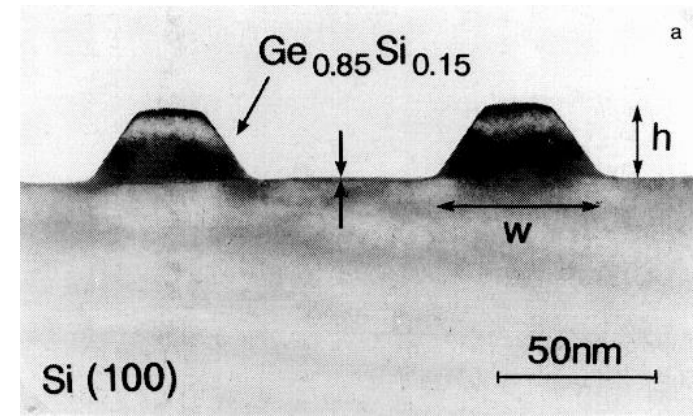


growth time < 1 s

Si 15.6 nm/Si_{0.995}C_{0.005} 5.2 nm



SiGe/Si QDs



LPE - summary

LPE



solution growth:

- low concentration of point defects
- high purity of the layers (segregation of impurities)
- selective area epitaxy easy
- wide range of compounds

epitaxy:

- ordered growth of multilayer crystalline structures

- technically simple (standard version)
- „cheap and easy”
- „safe” technique
- growth rate $\sim \mu\text{m}/\text{min}$
- growth of low-dimensional structures very difficult

disadvantages:

limitations due to equilibrium nature of LPE growth

- doping limited by phase diagram (e.g. GaAs:Mn)
- structures requiring a high supersaturation (GaAs/Si) difficult to fabricate
- systems with limited solubility in solid (phase separation) difficult to grow
- no *in situ* growth monitoring possible (some possibilities in LPEE)

**LPE considered as „old fashion” technology – wrong !!!
Every technology is important and valuable if properly used**

for further reading on LPE

Handbook of Crystal Growth, Ed. D.T.J. Hurle
vol. 3, Elsevier 1994

- E. Bauser *Atomic mechanisms in semiconductor Liquid Phase Epitaxy*
- M.B. Small, E.A. Giess and R. Ghez *Liquid Phase Epitaxy*

E. Kuphal *Liquid Phase Epitaxy* Appl. Phys. A52 (1991) 380.

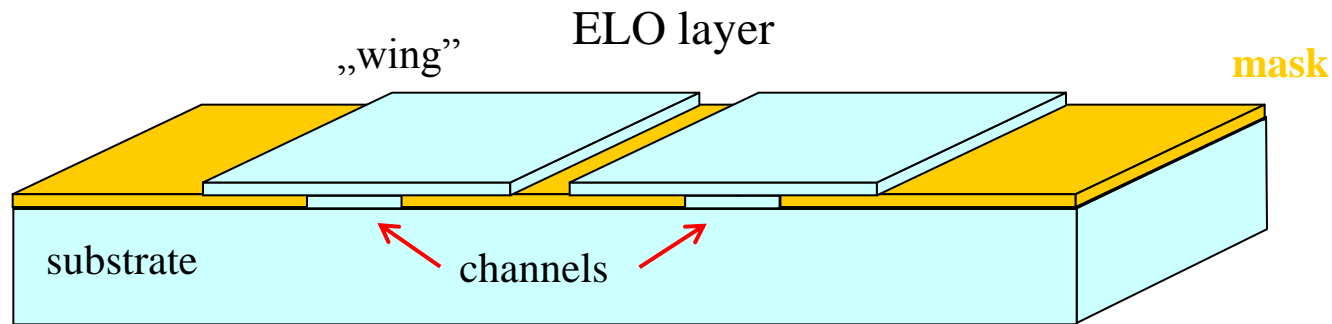
M.B. Small, I. Crossley *The physical processes occurring during liquid phase epitaxial growth*
J. Cryst. Growth 27 (1974) 35.

M.G. Astles *Liquid Phase Epitaxial Growth of III-V Compound Semiconductor Materials and their Device Applications*, IOP Publishing 1990.

B. Pamplin (ed.) *Crystal growth*, Pergamon, 1974

K. Sangwal (ed.) *Elementary Crystal Growth*, SAAN Publishers, 1994.

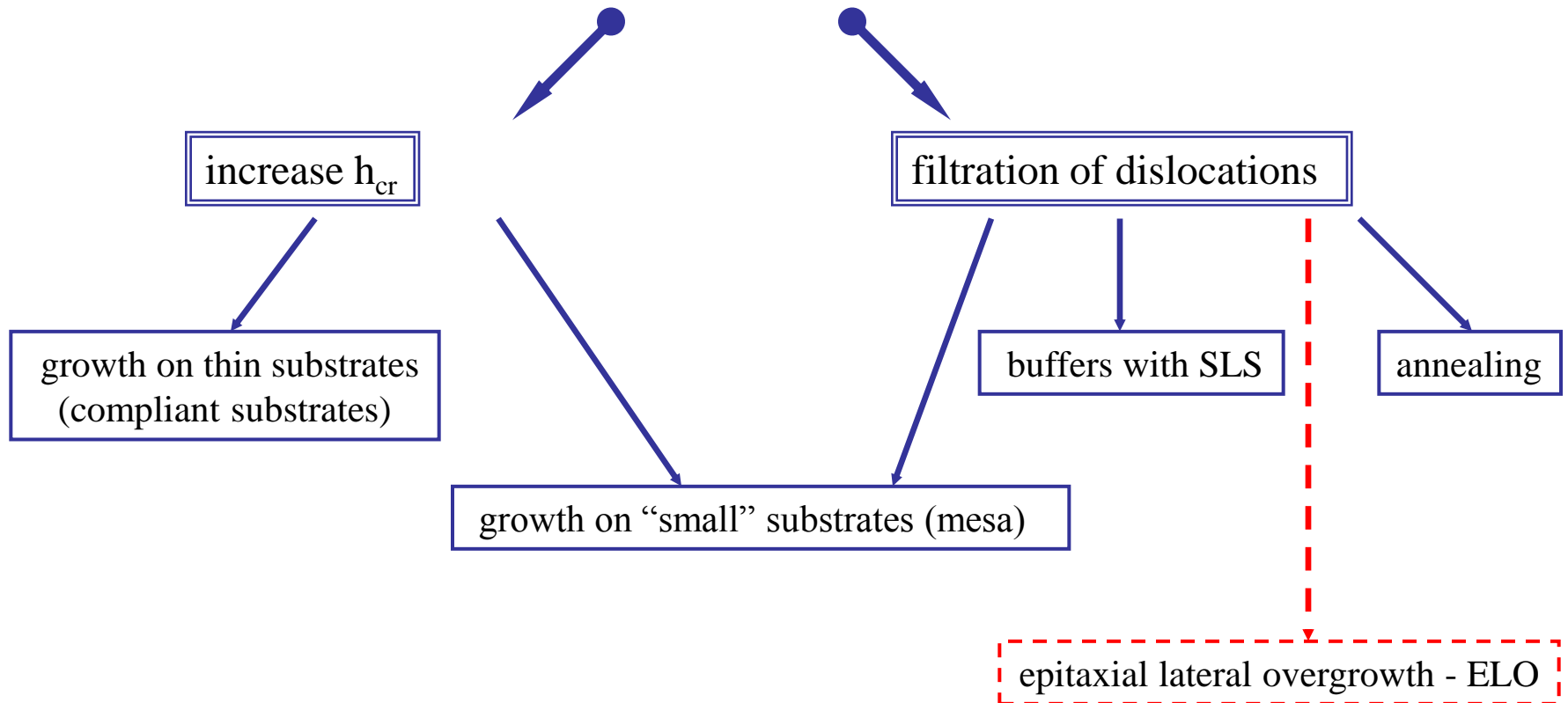
Epitaxial Lateral Overgrowth (ELO)



requirements:

- **high growth selectivity (no nucleation on the mask)**
- **fast lateral (horizontal) growth V_{lat}**
- **slow normal (vertical) growth V_{ver}**

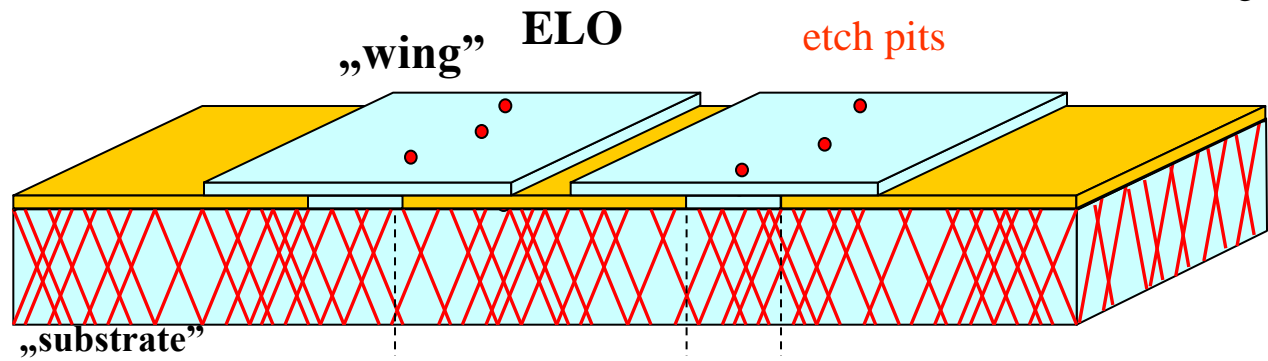
Methods to reduce defect density in lattice mismatched epitaxial structures - summary



There are no universal method to reduce dislocation density in lattice mismatched heterostructures;
 The best way is to avoid lattice mismatch – find the suitable substrate !!!

ELO = a method to reduce dislocation density in epitaxial structures

mask: SiO₂, Si₃N₄,
W, ZrN, grafit, ...



S

W

MOVPE GaN: S = 5 – 20 μm; W = 2 - 5 μm
LPE GaAs: S = 100 – 500 μm; W = 6 - 10 μm



ELO

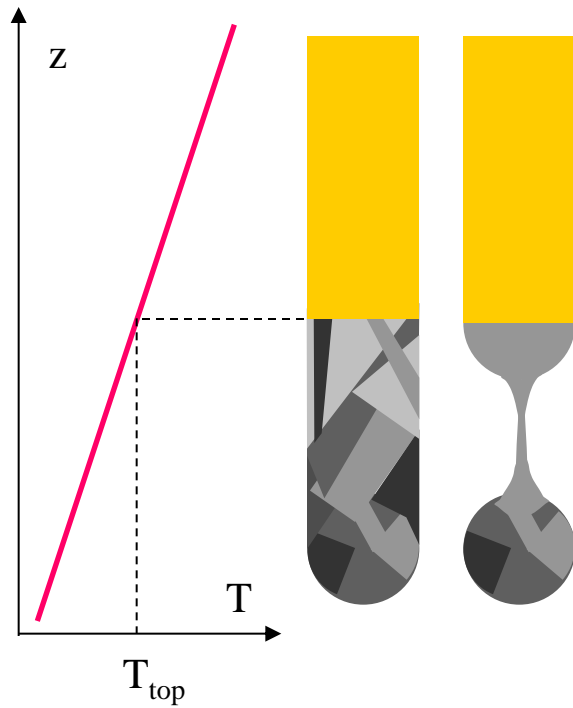
	GaN GaAs A _x B _{1-x} C		
buffer	GaN	GaAs	A _x B _{1-x} C
substrate	sapphire	Si	binary

new class of substrates with designed lattice parameter $a = f(x)$

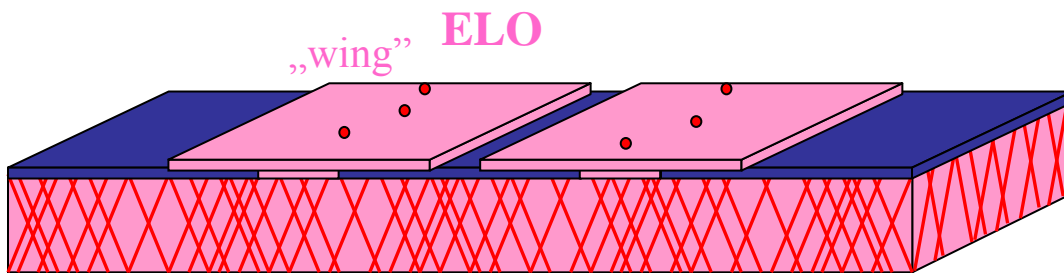
wide and thin ELO layers needed

dislocation filtration in ELO – is it a new idea?

Necking in Bridgman growth



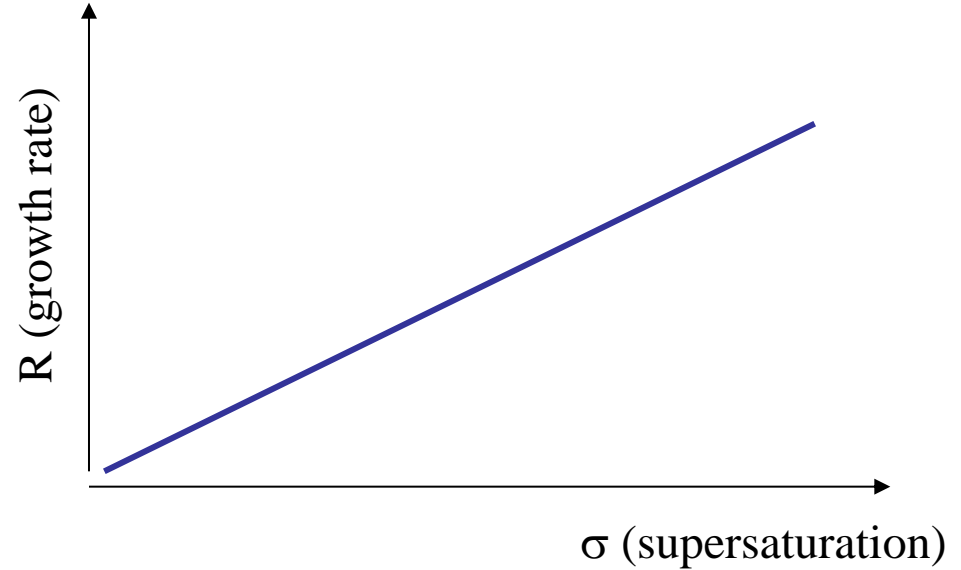
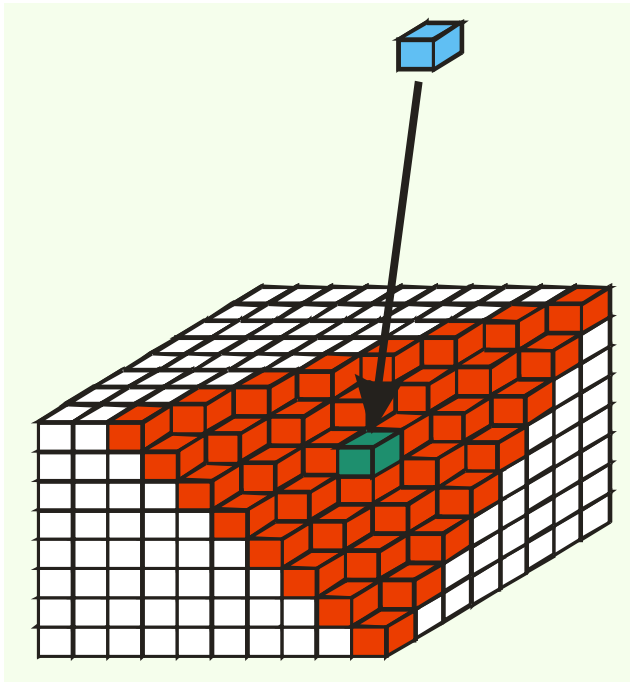
Cu crystal – Czochralski growth



recipe: take from the seed info on crystal lattice; do not take defects;

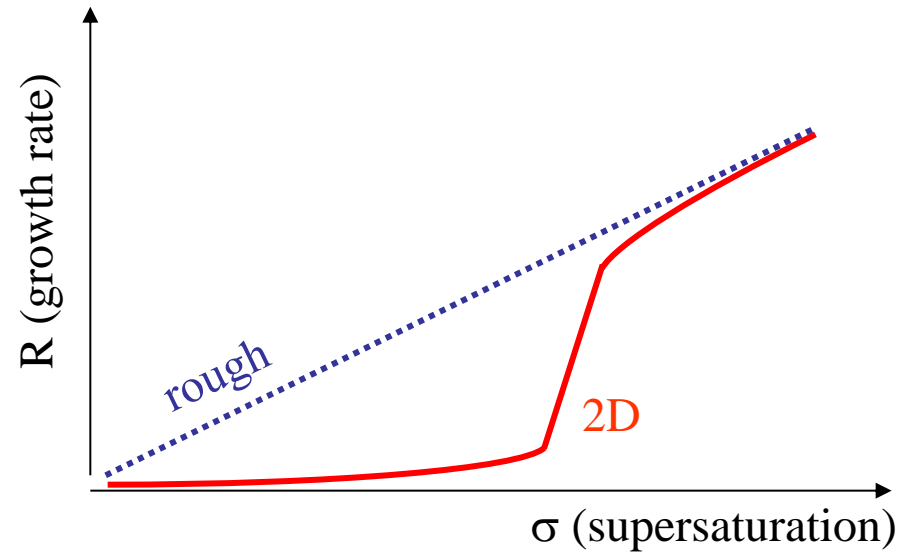
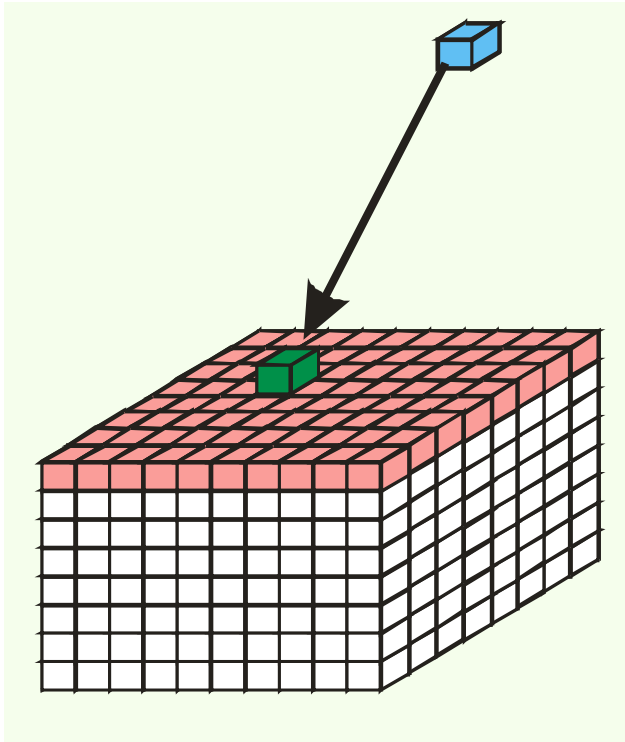
Growth rate of various crystal faces (*Krukowki's lecture*)

atomically rough surface



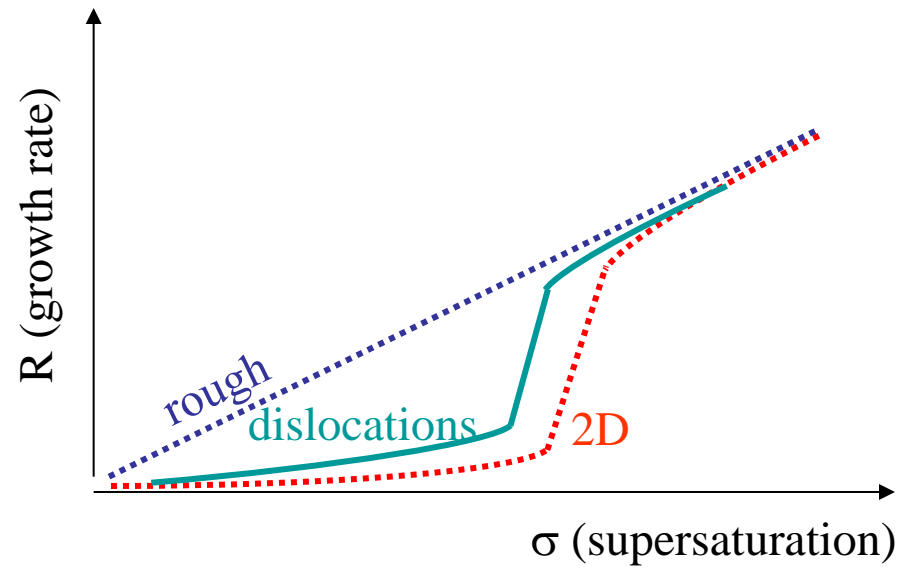
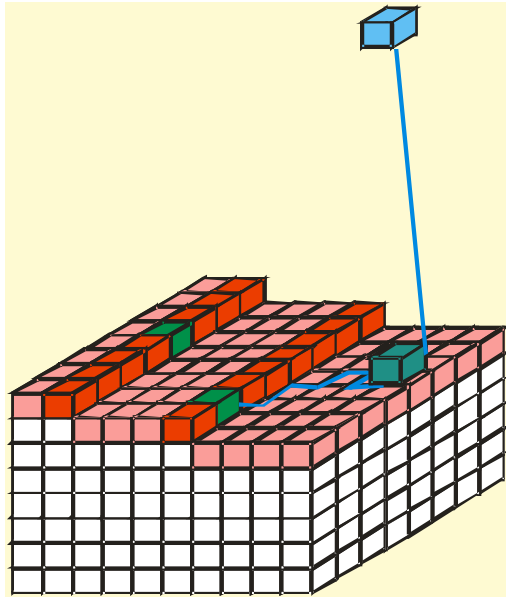
Growth rate of various crystal faces (*Krukowki's lecture*)

atomically smooth surface w/o dislocations (2D nucleation)

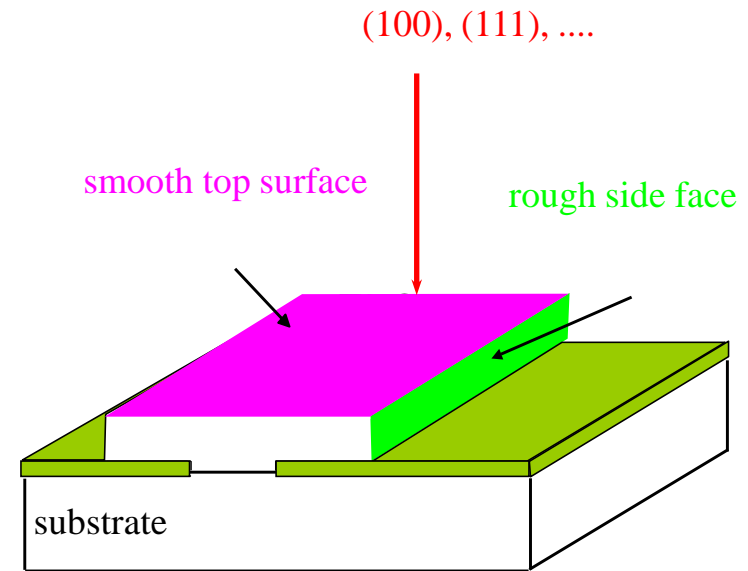
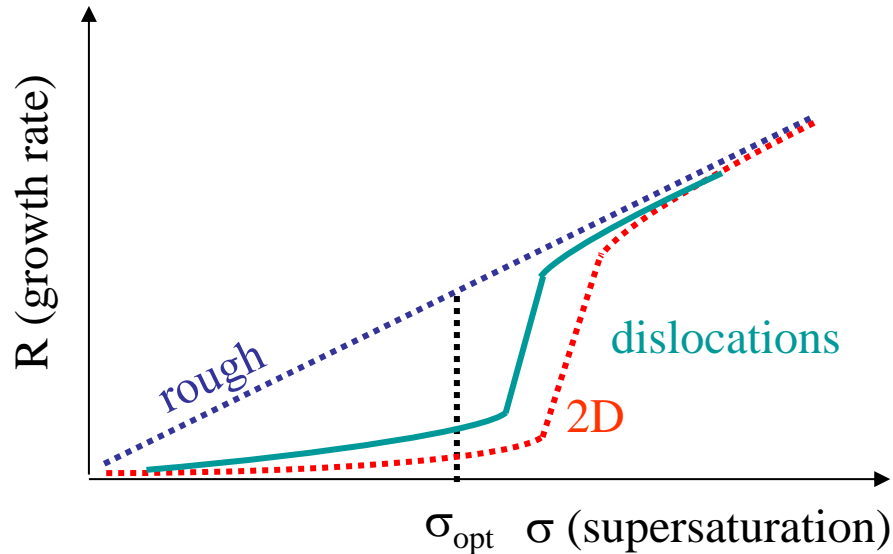


Growth rate of various crystal faces (*Krukowki's lecture*)

atomically smooth surface with dislocations



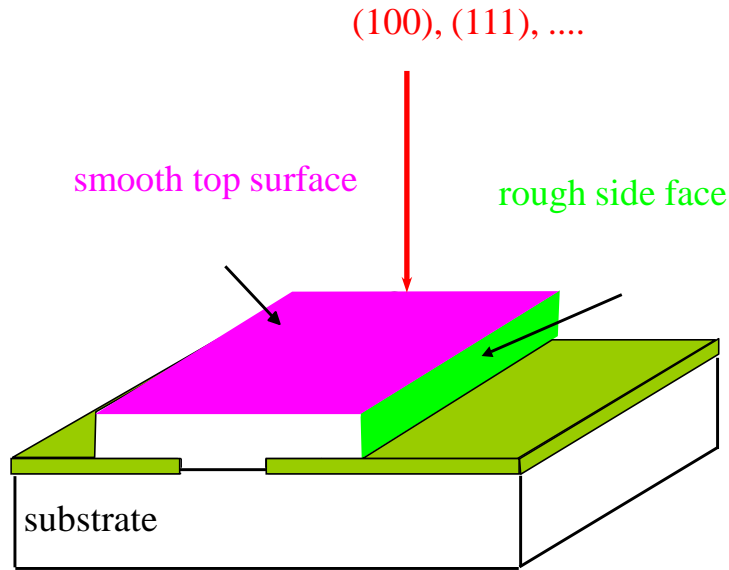
Mechanism of ELO growth



to get a high aspect ratio we need:

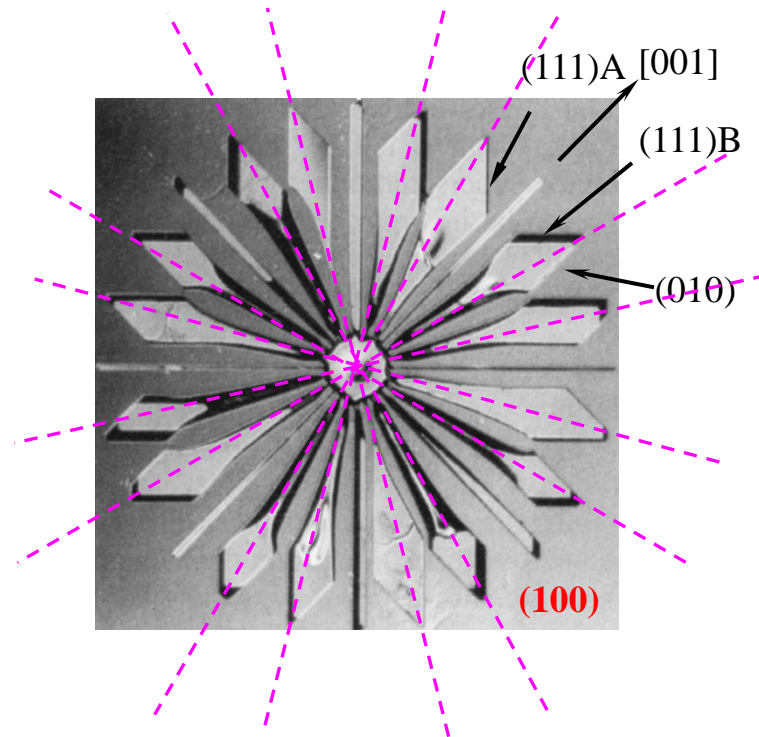
- smooth top surface (low normal growth rate V_{ver})
- rough side face (high lateral growth rate V_{lat})
- adjust supersaturation to σ_{opt} - LPE perfect !!!
 - VPE, MOVPE, HVPE - possible
 - MBE ??? problems

Mechanism of ELO growth



Zytkiewicz *Cryst. Res. Technol.* 1999

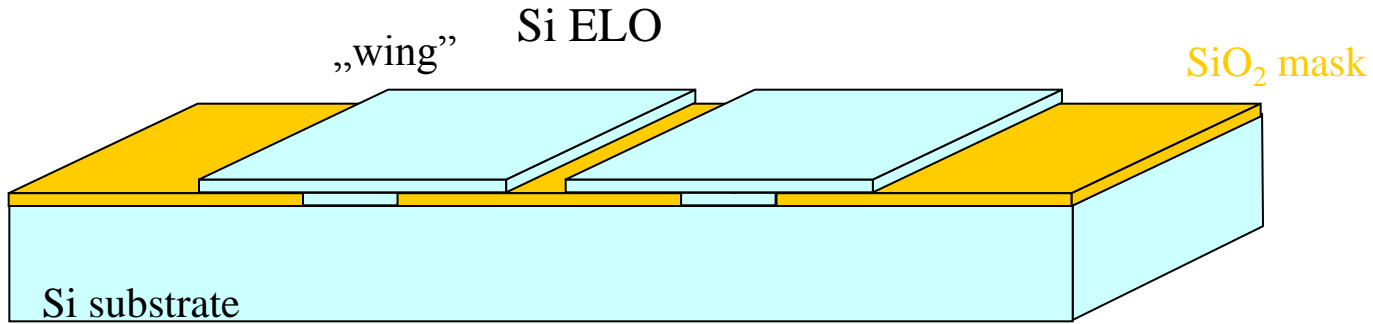
GaAs layer on (100) GaAs by LPE



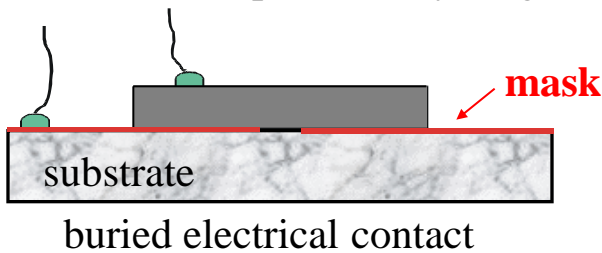
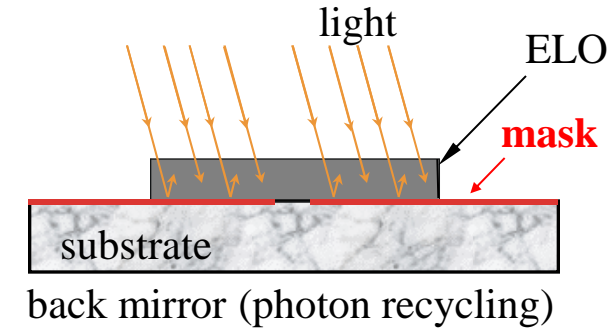
8 equivalent window directions on substrate without miscut

1 preferential window orientation on substrate with surface miscut

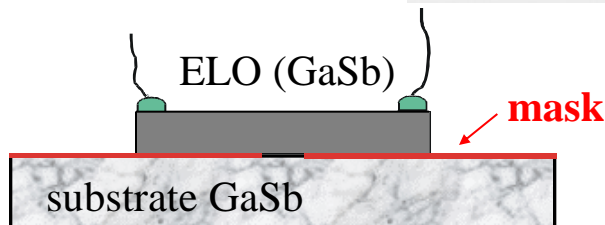
Application of ELO structures grown by LPE



- silicon-on-insulator structures
- buried electrical contact/mirror

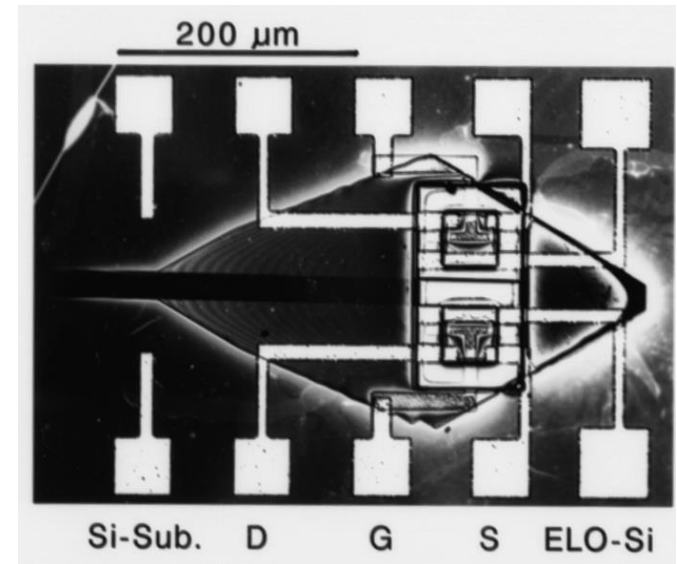


- electrical separation of epilayer from the substrate



MOS transistor on ELO Si/SiO₂

Bergmann et al. Appl. Phys. A (1992)



ELO Si/SiO₂/Si by LPE

E. Bauser et al. Max-Planck Inst. Stuttgart

origin of strange ELO shape
- the case of dislocation-free Si substrate

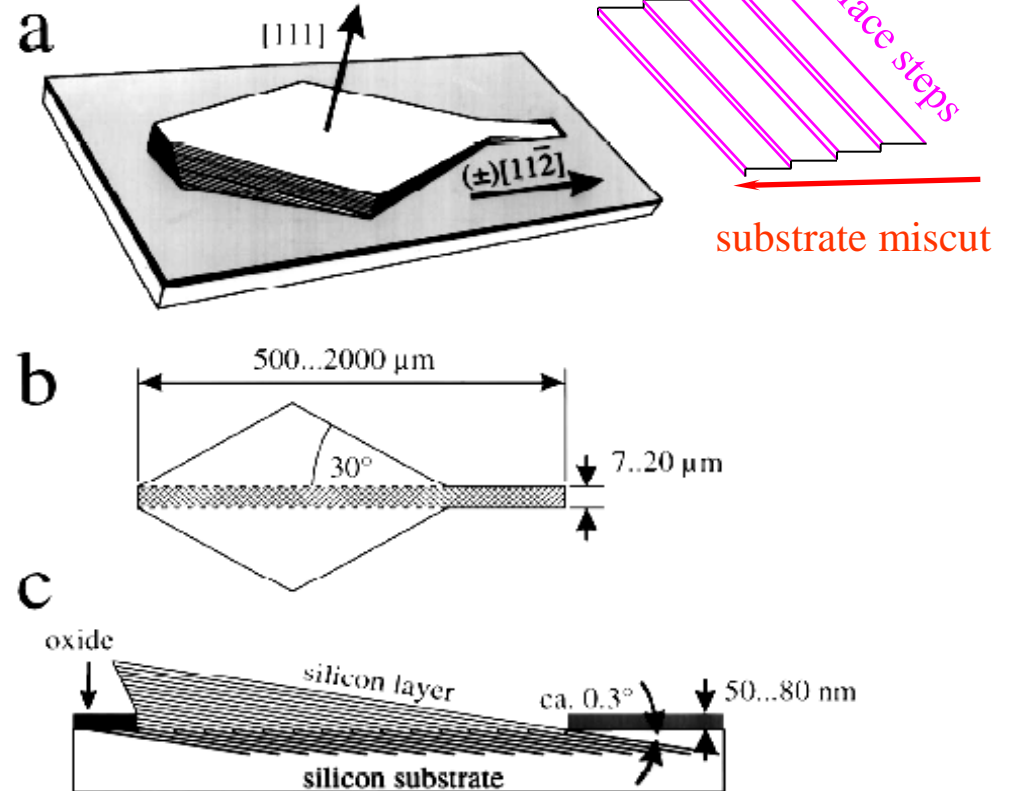
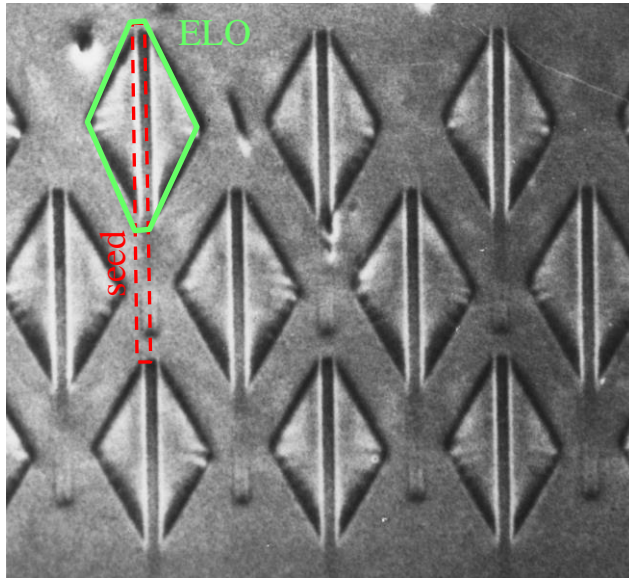
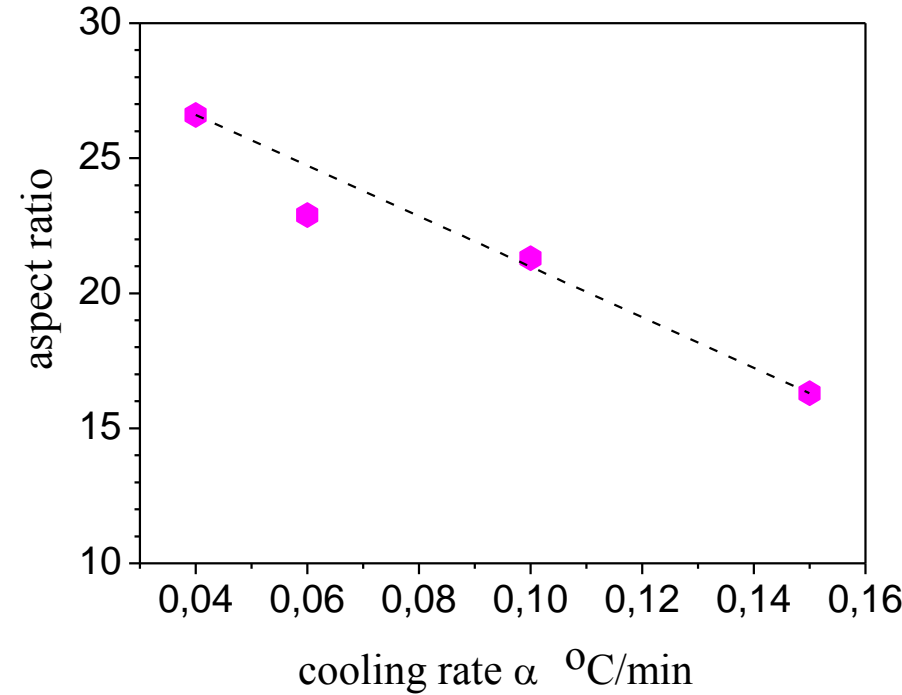
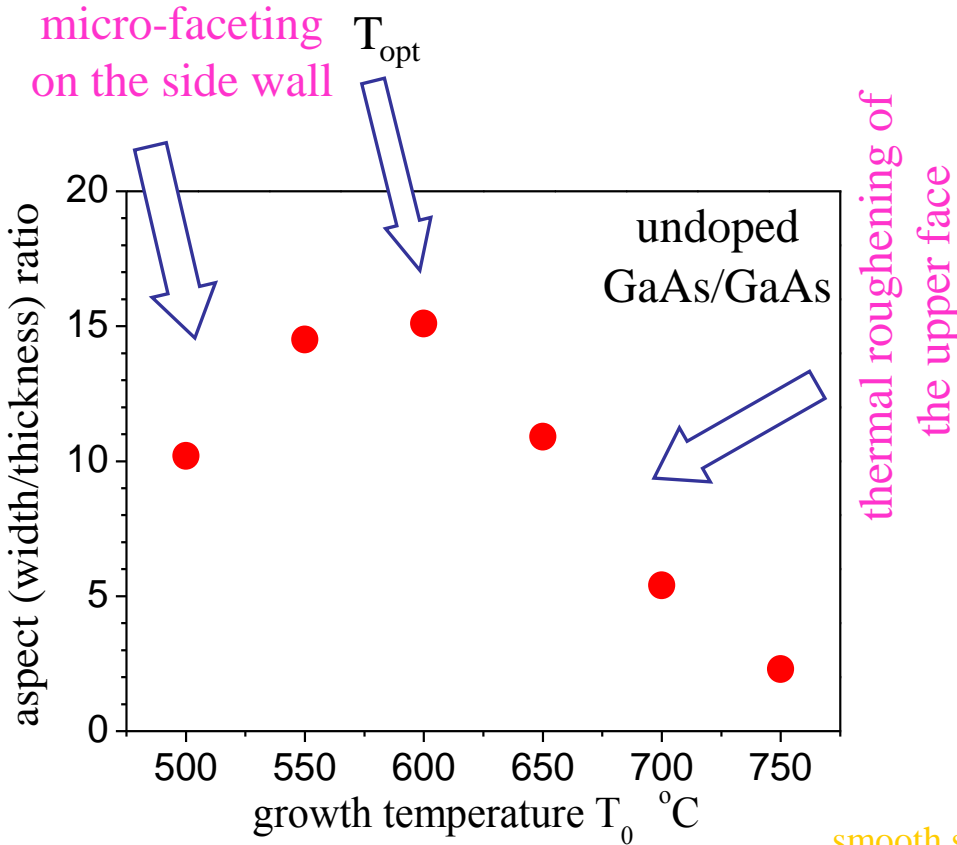


FIG. 1. Silicon layers grown from oxide-free seeding areas on {111} Si. Substrate partially masked by thermal oxide. Substrate off-orientation 0.3° in the [112] direction (schematic view). The crosshatched area in (b) indicates the seed window.

ELO – optimization of supersaturation in LPE

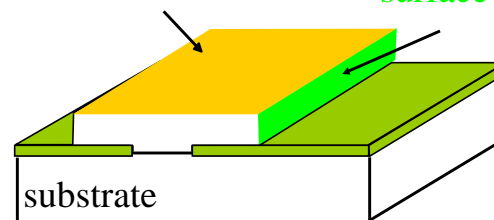
growth temperature

ELO GaAs - cooling rate



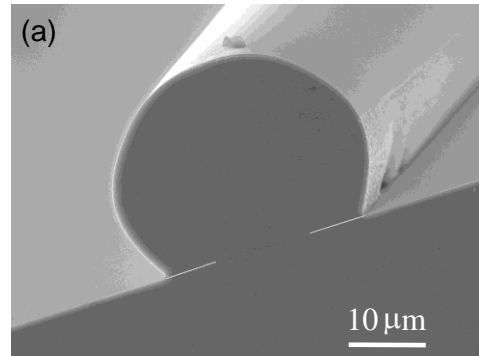
smooth surface

rough surface

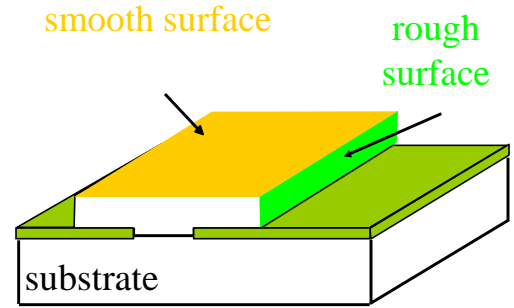
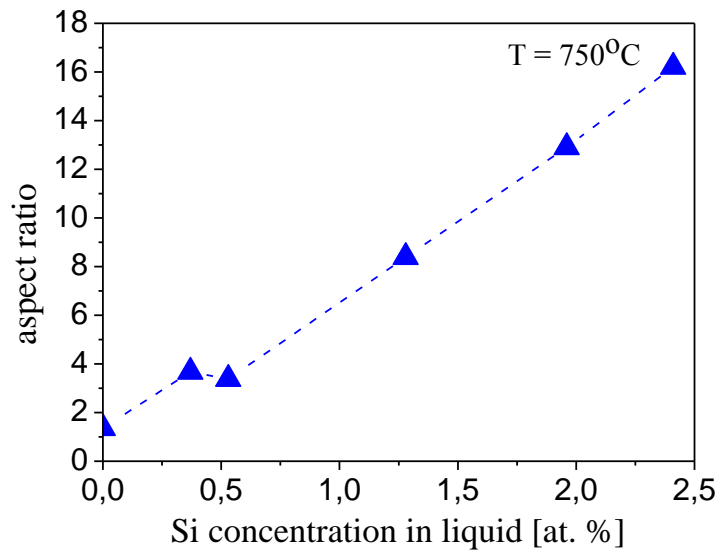
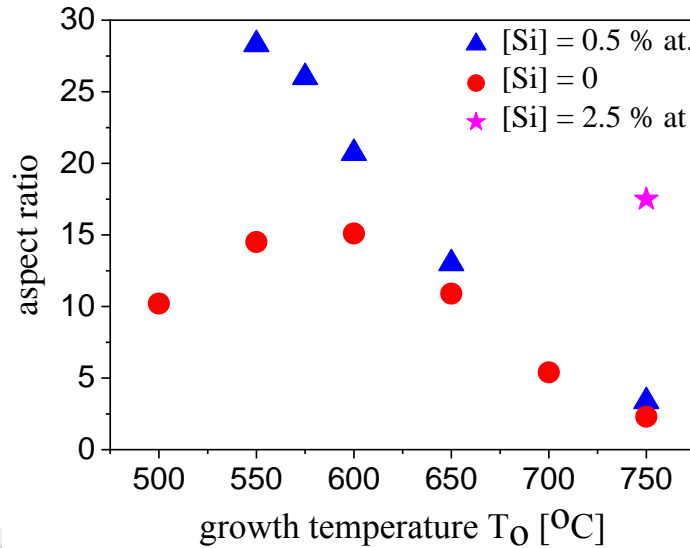
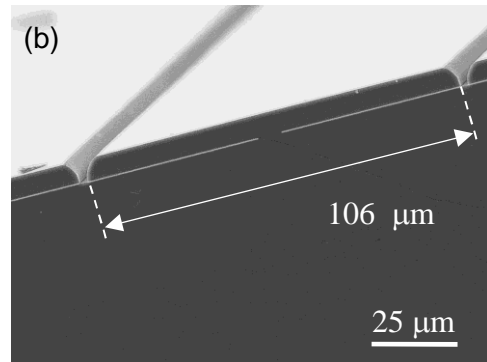


ELO – influence of doping on the aspect ratio (LPE)

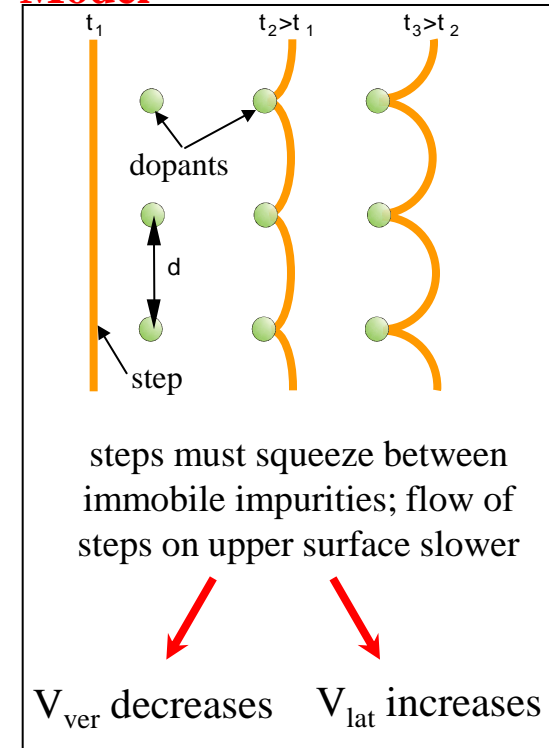
ELO GaAs - undoped



ELO GaAs - Si doped



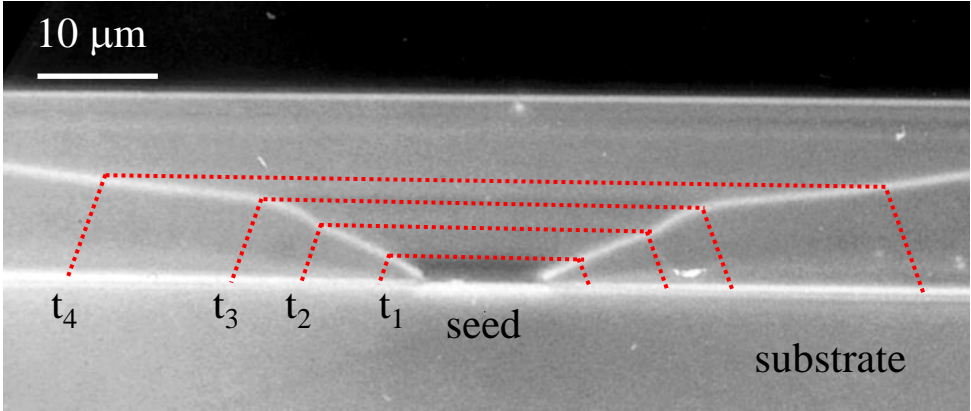
Model



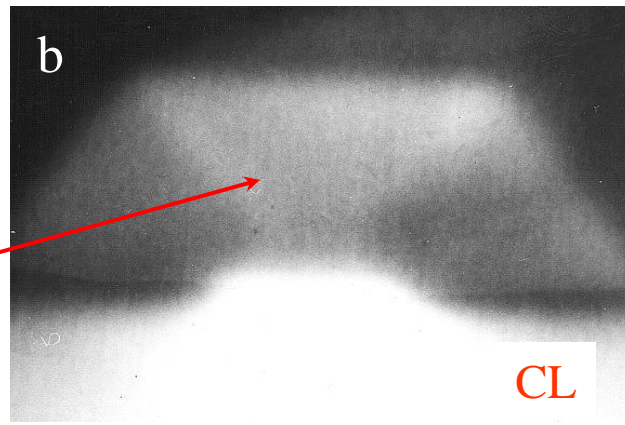
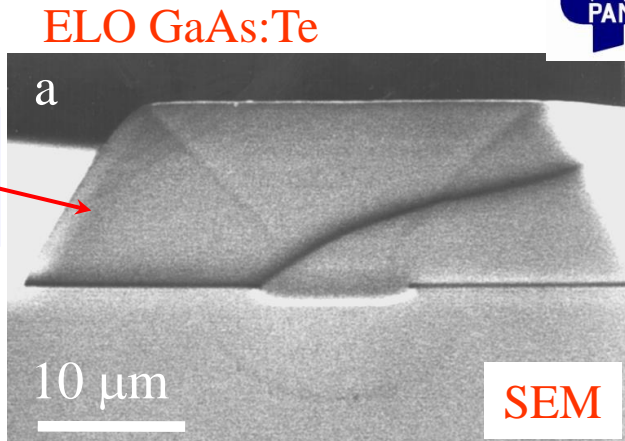
ELO by LPE – dopant incorporation

doping vs. growth rate \leftrightarrow lecture by T. Stupiński

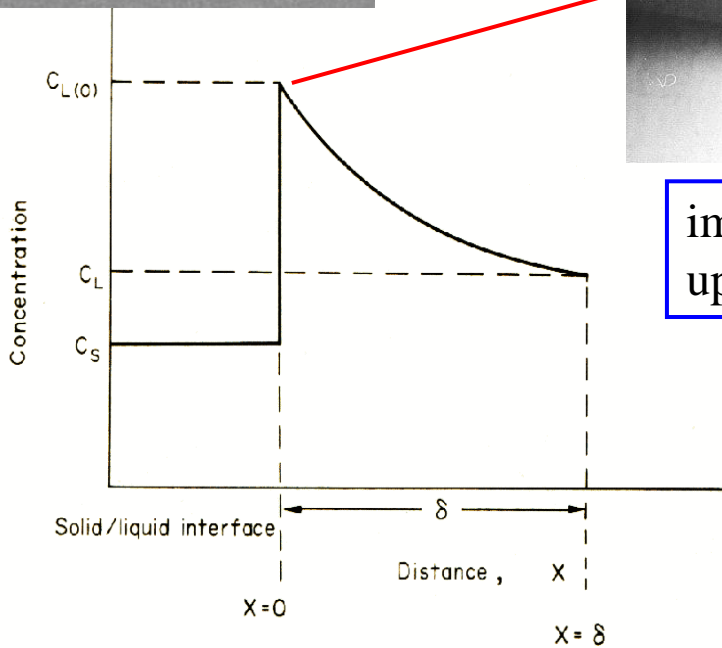
how ELO develops ...



rough face – no segregation k_0

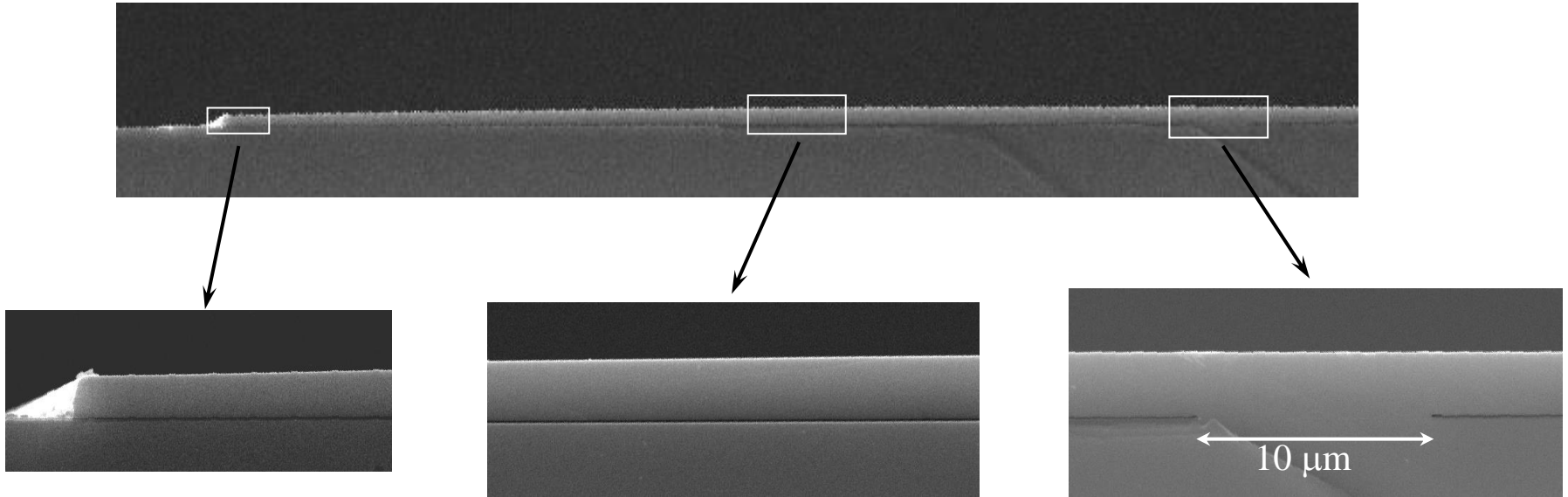


impurity segregation at upper face k_{eff}



GaAs ELO layers on GaAs substrates by LPE

$L = 172 \mu\text{m}; t = 2.8 \mu\text{m}$



thickness $t = 2.8 \mu\text{m}$
width of the wing $L = 172 \mu\text{m}$

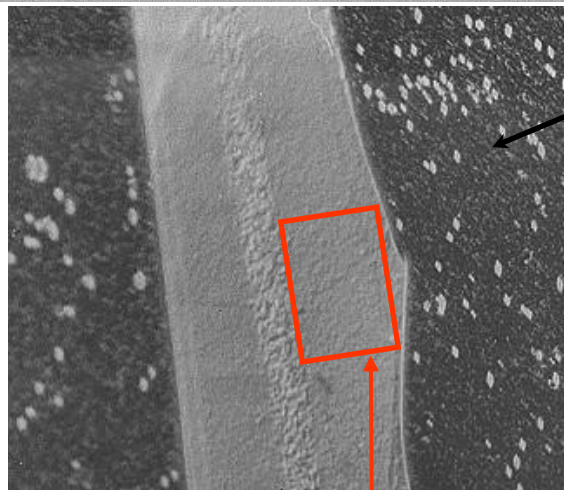
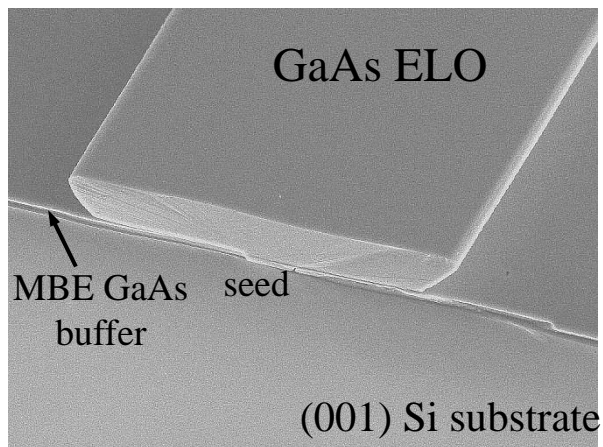


aspect ratio $2L/t = 126$

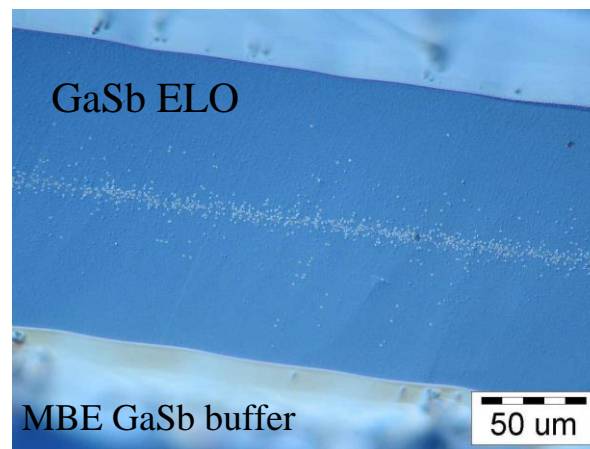
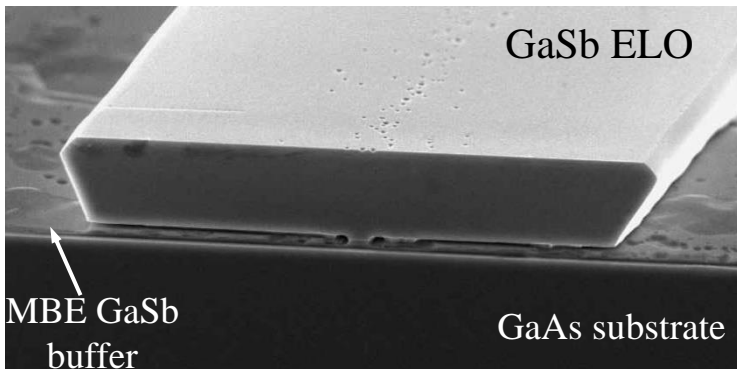
Why the layer is thinner at the edge?
nonuniform growth ...
bowing ...

Filtration of dislocations in ELO - examples

LPE - GaAs/Si



LPE - GaSb/GaAs

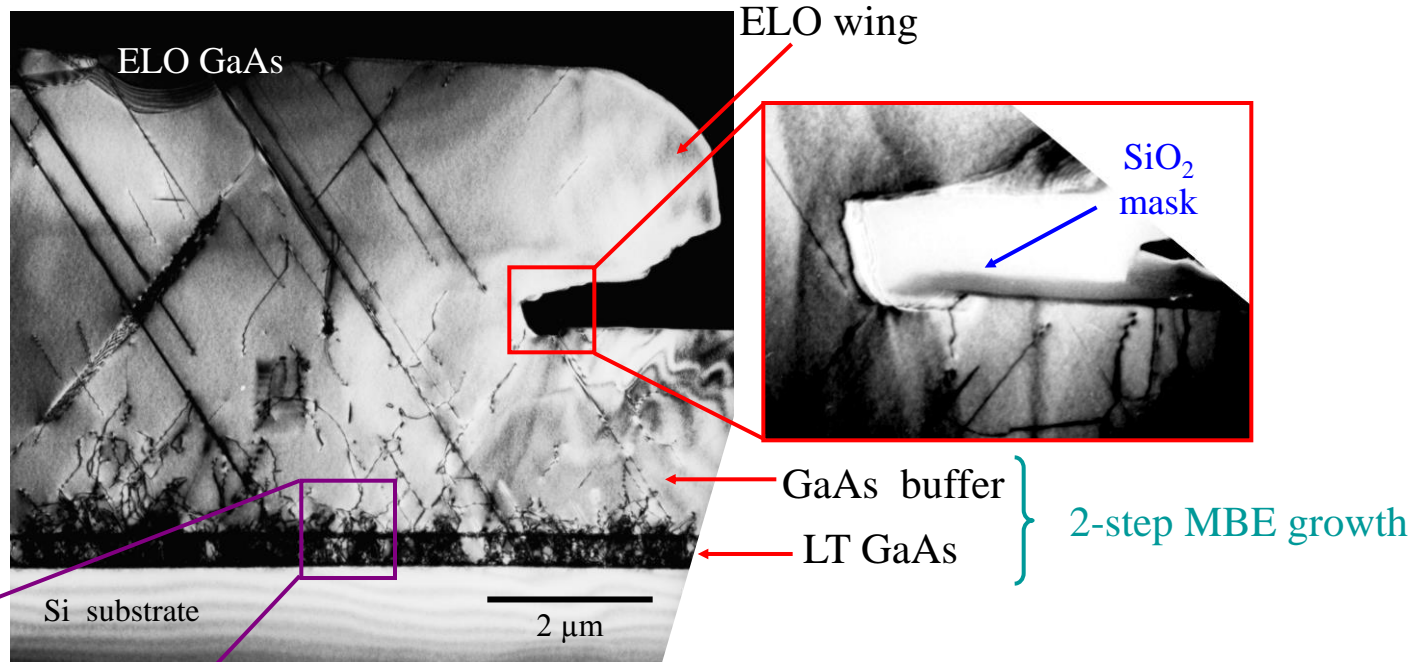


EPD > 10^{-8} cm⁻²

after etching

MBE grown GaAs/Si (GaSb/GaAs) templates; ELO by LPE

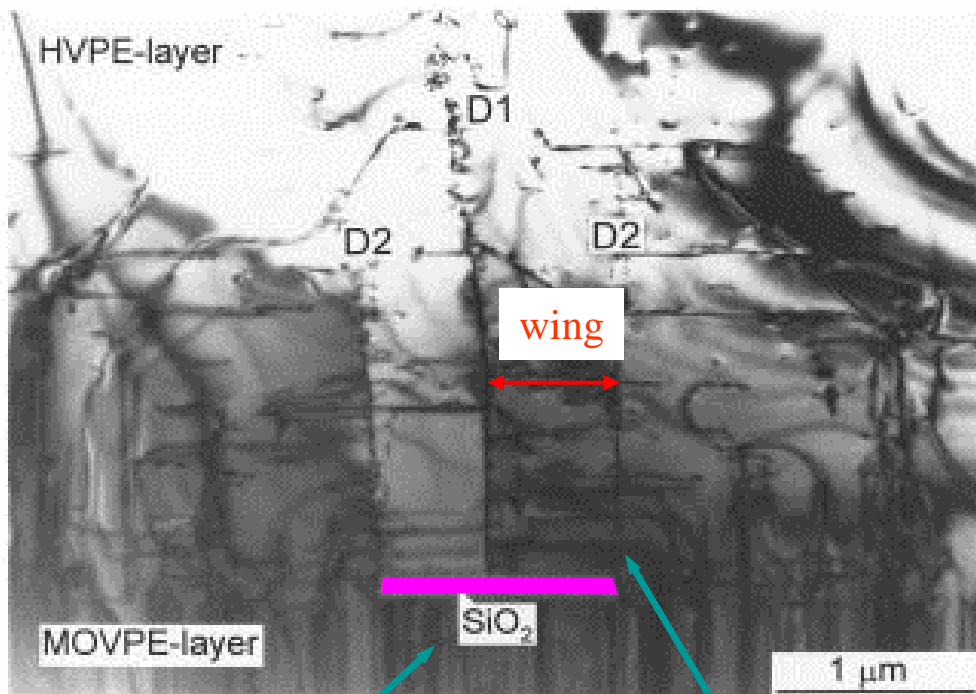
Filtration of dislocations in ELO: TEM of GaAs/Si



Filtration of dislocations in ELO: TEM of HVPE GaN/sapphire

Sakai et al. APL 1998

TEM



dislocations blocked
by the mask

bending of TD's
in the window area !!!

width of the ELO wing

	MOVPE GaN*	LPE GaAs/Si**	LPE GaAs/GaAs
wing width L	$\leq 5 \mu\text{m}$	$\leq 90 \mu\text{m}$	$\leq 200 \mu\text{m}$

* Fini et al. JCG (2000) ** Chang et al. JCG (1998)

Filtration of dislocations in ELO: cathodoluminescence

Zytewicz *Thin Solid Films* 412 (2002) 64

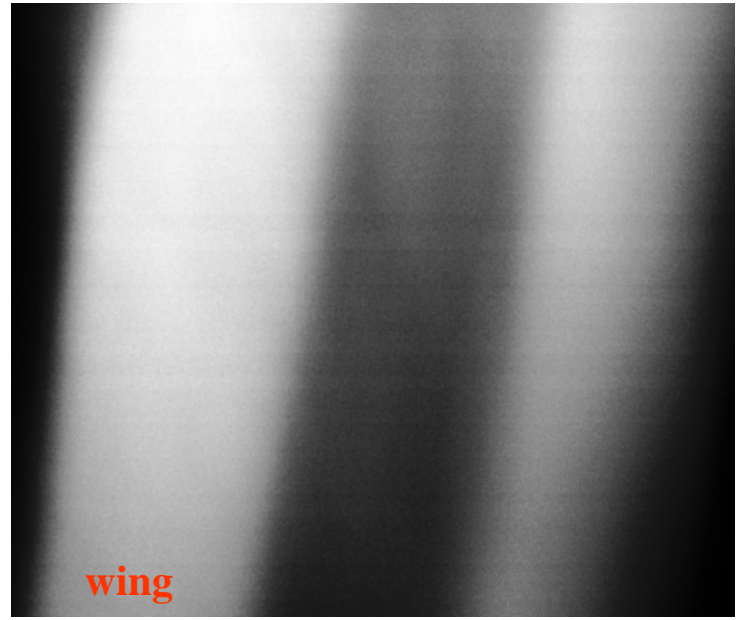
Yu et al. *MRS Internet Nitride Semicond. Res.* 1998

LPE GaAs/Si

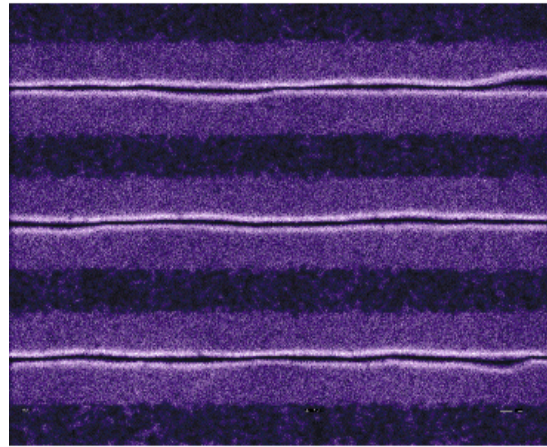
MOVPE GaN on sapphire

integrated CL

band edge emission 365 nm



wing
wing

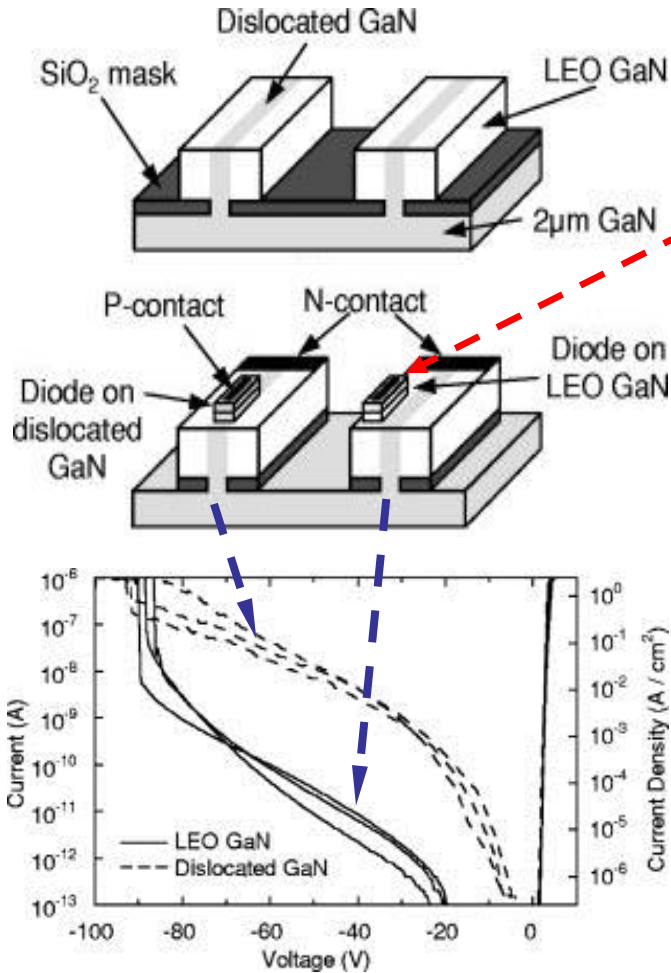


Window (3 μm)
SiO₂ (5 μm)
Window (3 μm)
SiO₂ (5 μm)
Window (3 μm)
SiO₂ (5 μm)
Window (3 μm)

↑
GaAs grown over the seed

ELO structures for devices

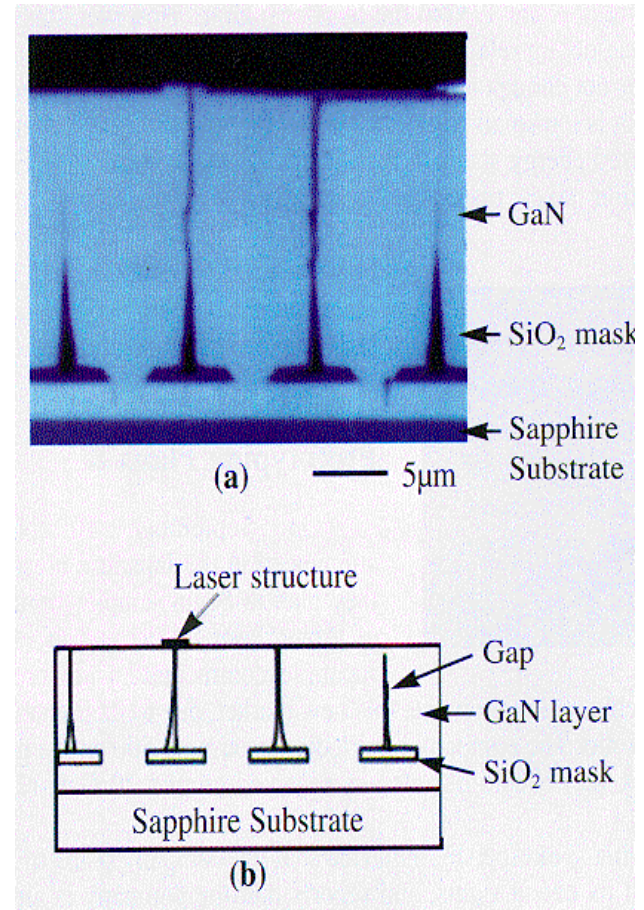
Kozodoy et al. APL 1998



large leakage current due to TD

Semicond. Res. 4S1, G1.1 (1999)

CW RT blue LD - Nichia



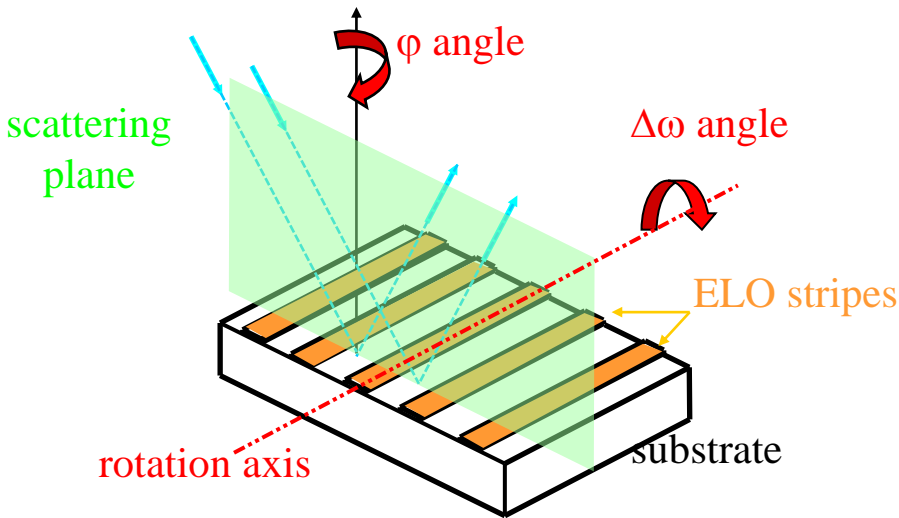
on the wing
on the window

$j_{th} = 3 \text{ kA/cm}^2$
 $j_{th} = 6-9 \text{ kA/cm}^2$

Strain in ELO layers

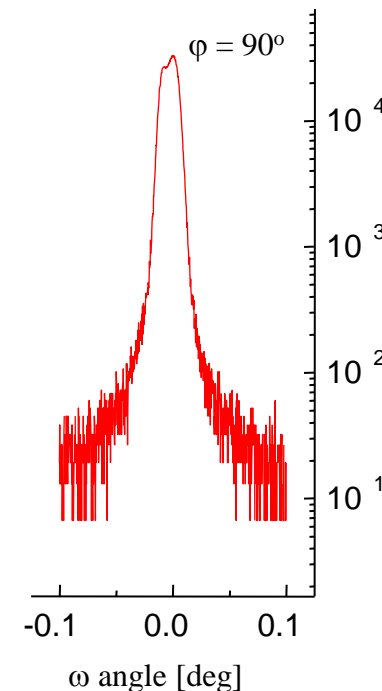
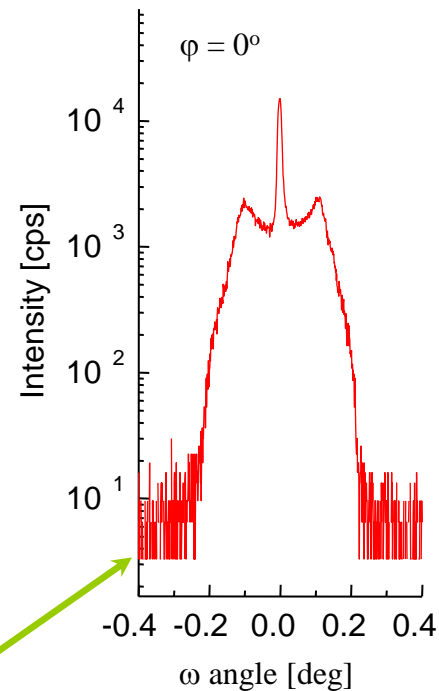
XRD – lecture by M. Leszczyński

XRD geometry



ELO GaAs on SiO₂-coated GaAs

Zytkiewicz et al. JAP 1998

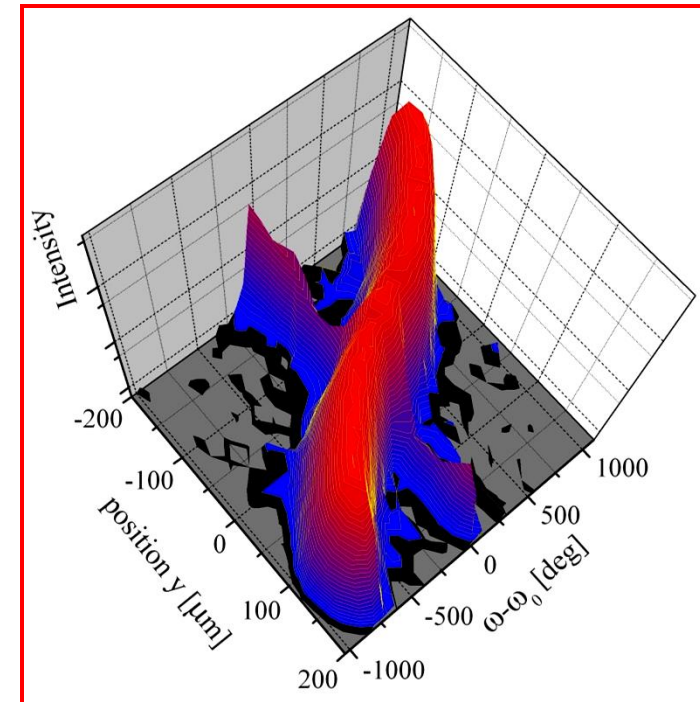
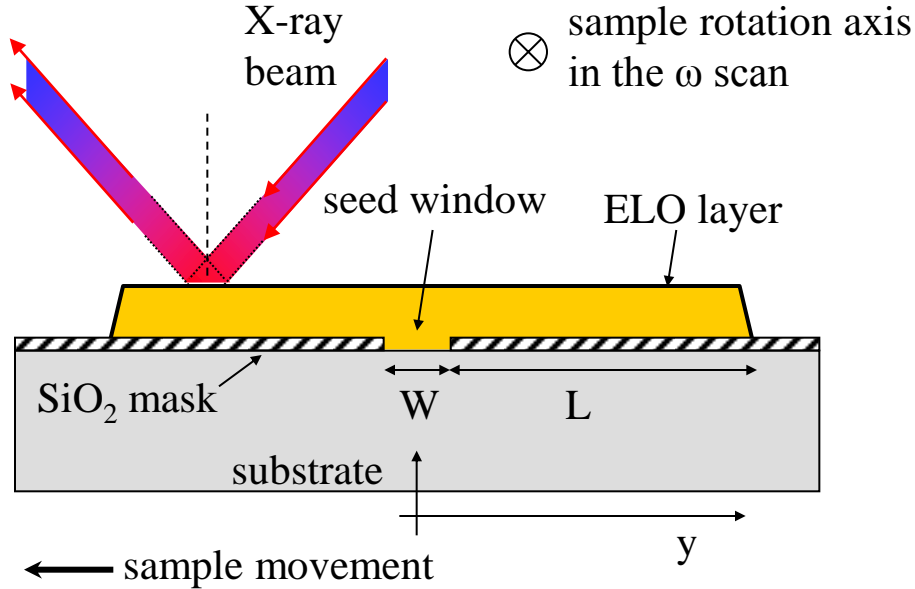


broadening of the RC:

- different values of lattice parameters ?
- different orientations of the ELO stripes ?
- bowing – direction ?

“typical” GaAs epilayer

Strain in ELO layers – local XRD



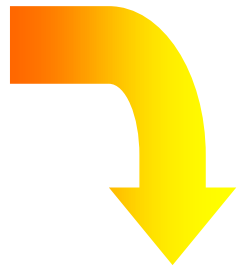
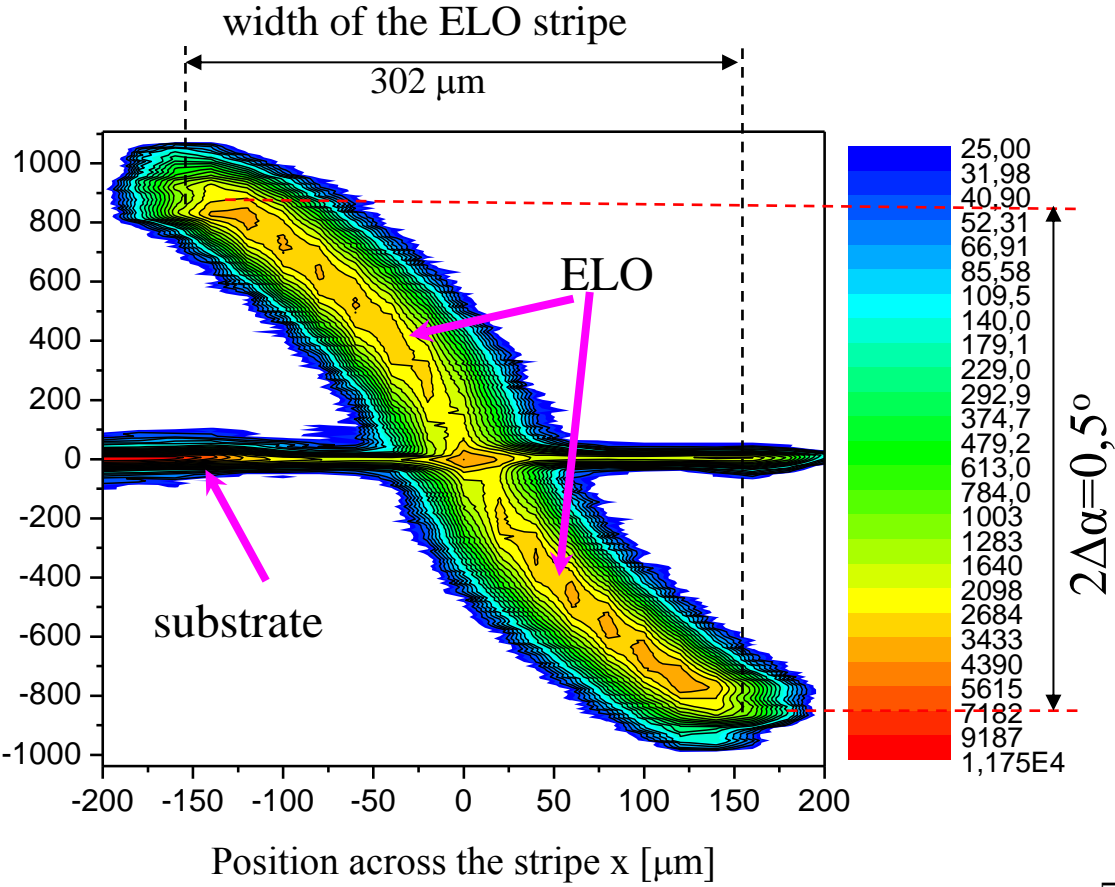
X-ray beam $5 - 10 \mu\text{m} \times 0.5 - 10 \text{mm}$

sample movement step $5 - 20 \mu\text{m}$

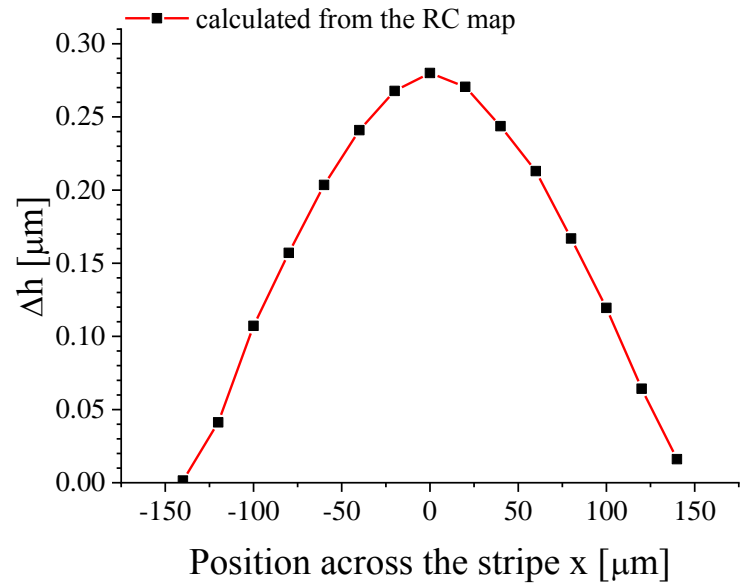
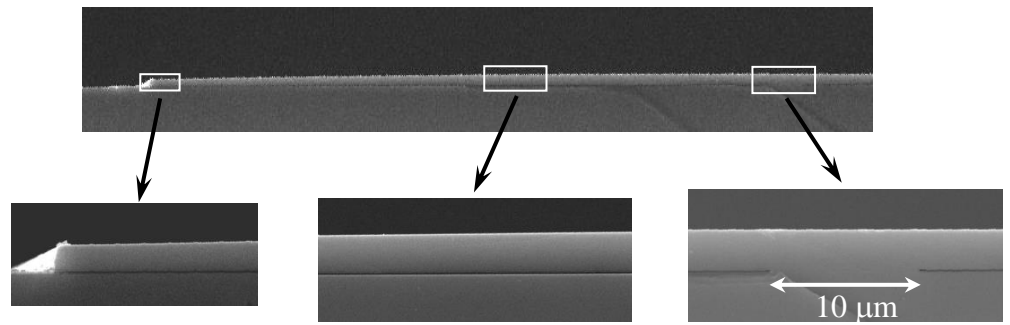
RC, RSM, ... measured *locally* → Rocking Curve mapping

Strain in ELO layers – local XRD

Czyzak et al. Appl. Phys. A 2008

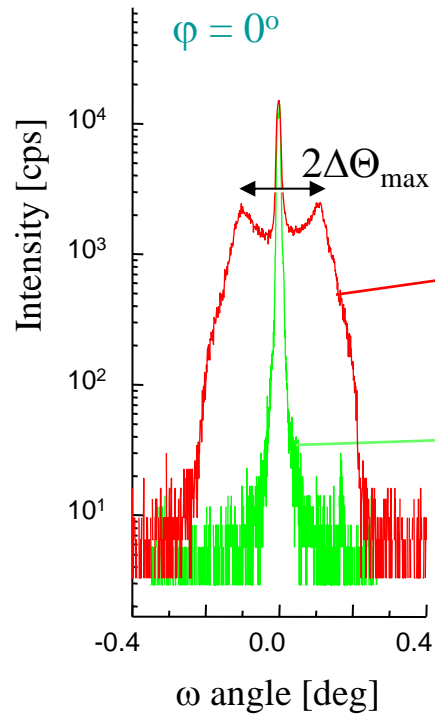


shape of (001) GaAs planes



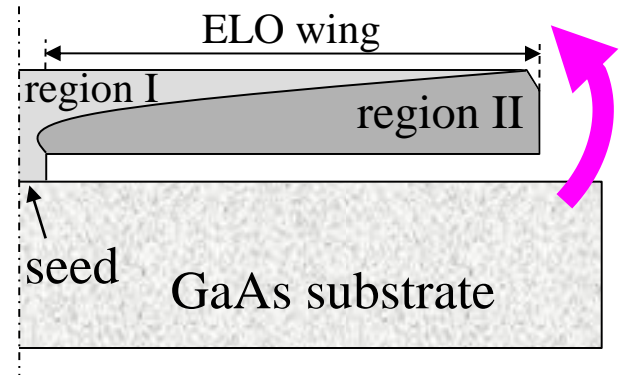
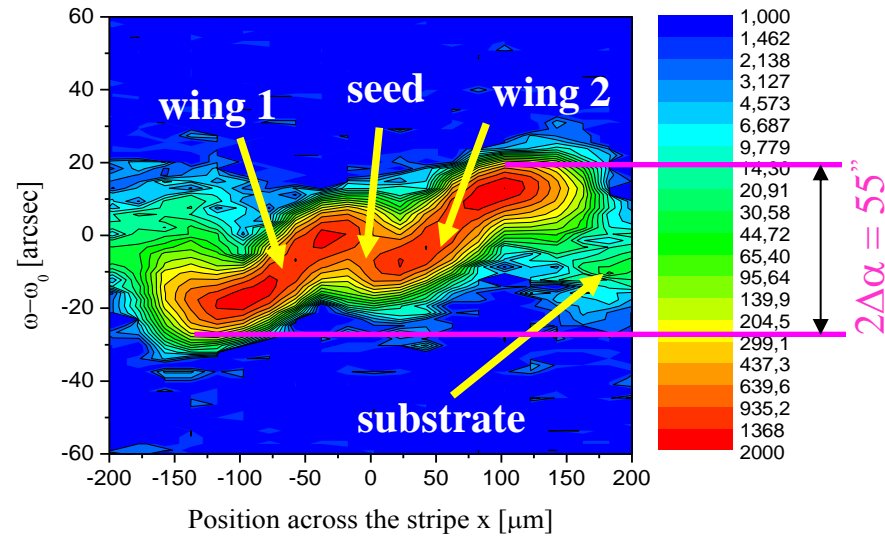
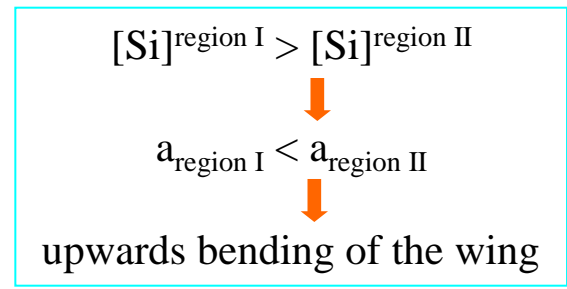
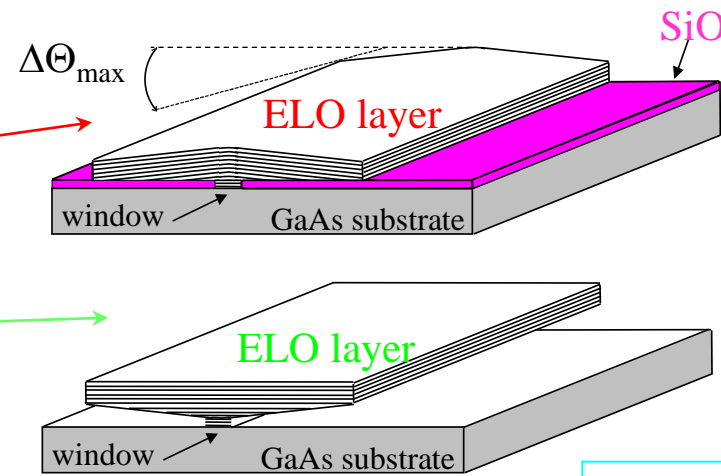
Bending of ELO layers

ELO GaAs on SiO₂-coated GaAs



as grown

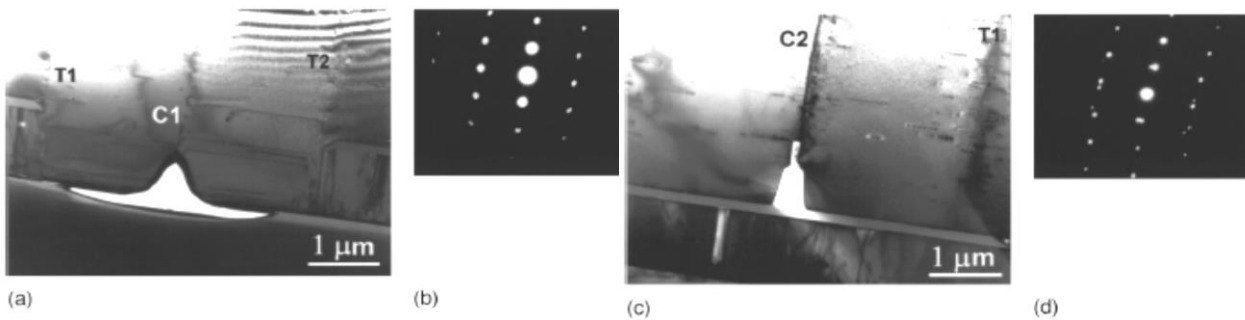
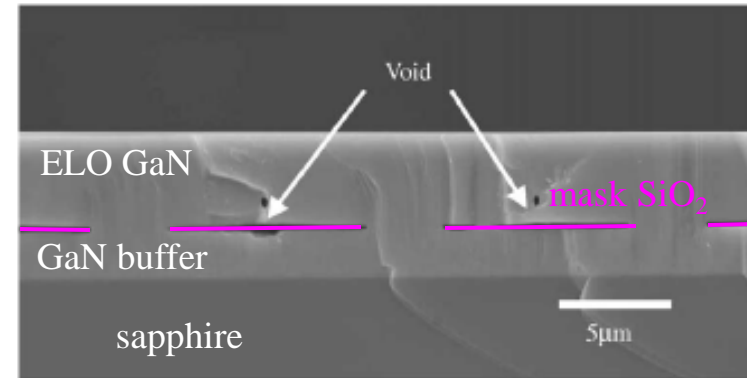
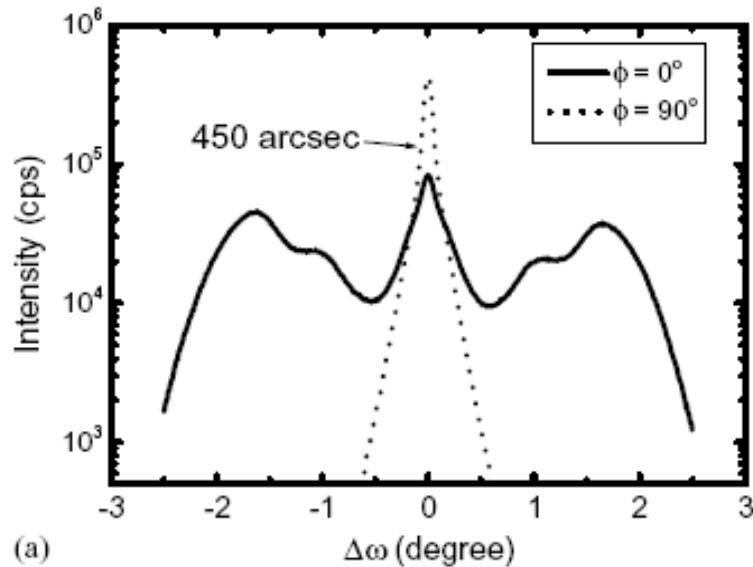
SiO₂ removed



Residual bowing due to nonuniform doping

ELO GaN on sapphire

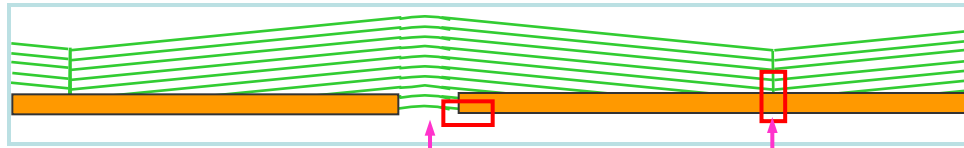
Kim et al. JCG 2002



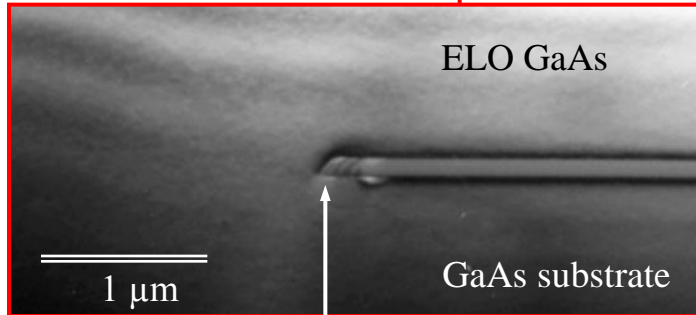
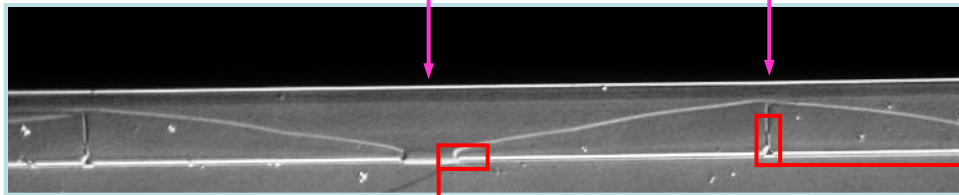
- tilt angle and tilt direction from electron diffraction in TEM
- synchrotron XRD

FIG. 2. TEM cross-section images and electron diffraction patterns taken from (a) and (b) window and (c) and (d) mask region.

Coalescence of ELO stripes

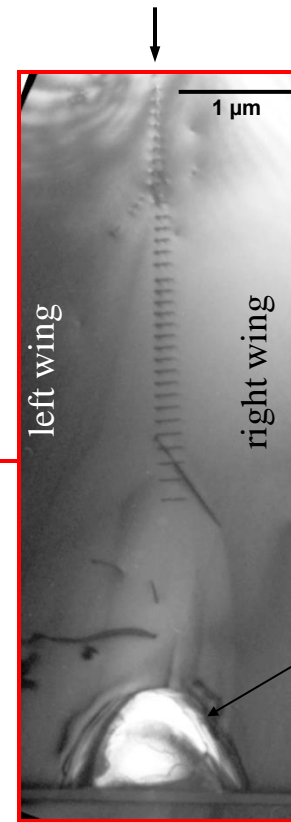


growth window front of coalescence



no dislocations
above the mask edge

low angle grain boundary



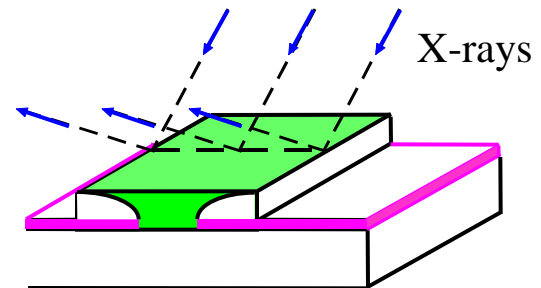
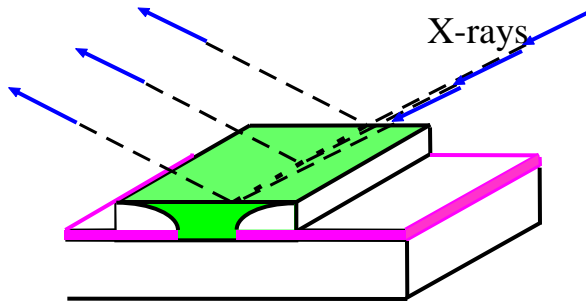
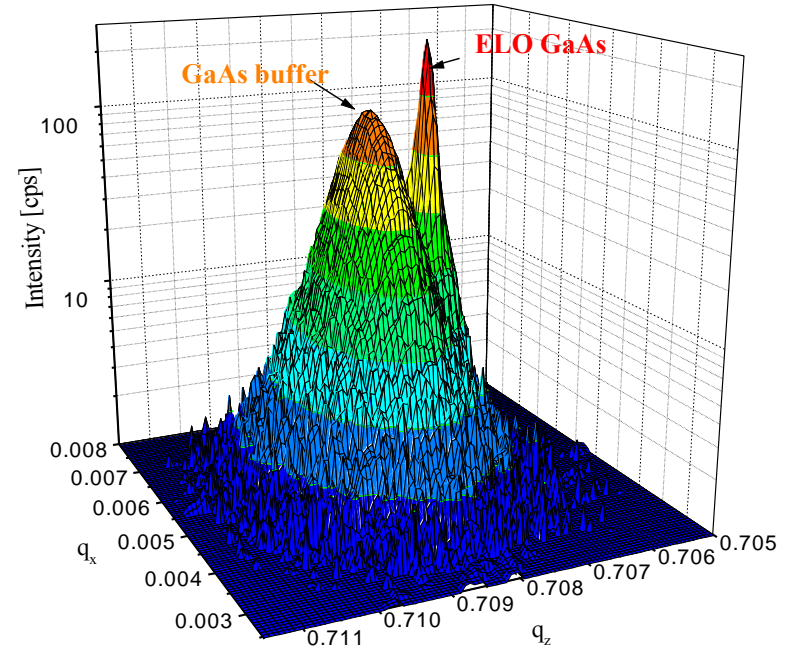
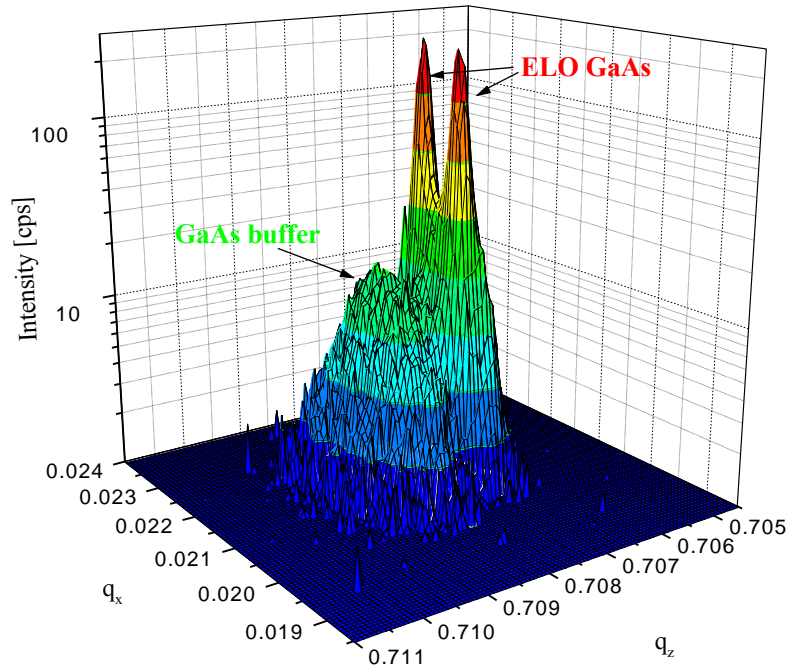
Zytkiewicz et al. JAP 2007

Similar effect in:

- ELO Si on Si - Banhart et al. Appl. Phys. 1993
- ELO GaN on sapphire - Sakai et al. APL 1998
- PE GaN on sapphire - Chen et al. APL 1999

.....

Thermal strain in ELO structures (GaAs/SiO₂/GaAs/Si)



Thermal strain in ELO structures (GaAs/SiO₂/GaAs/Si)

Zytkiewicz et al. APL 1999

Our model:

direction of tilt \longleftrightarrow sign of thermal strain in the buffer

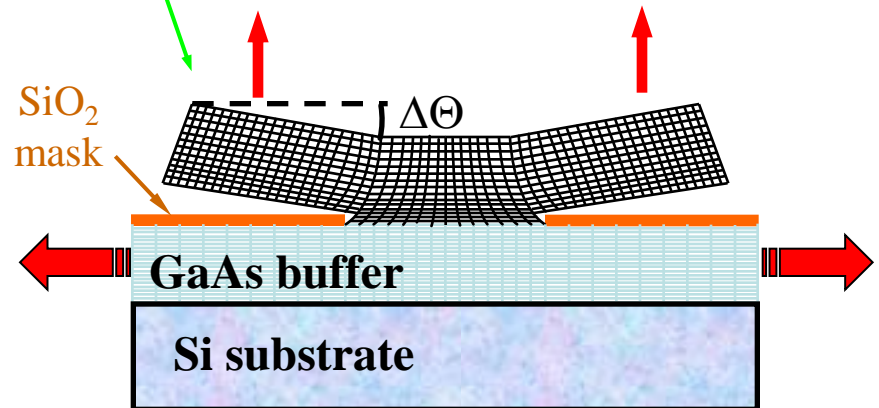
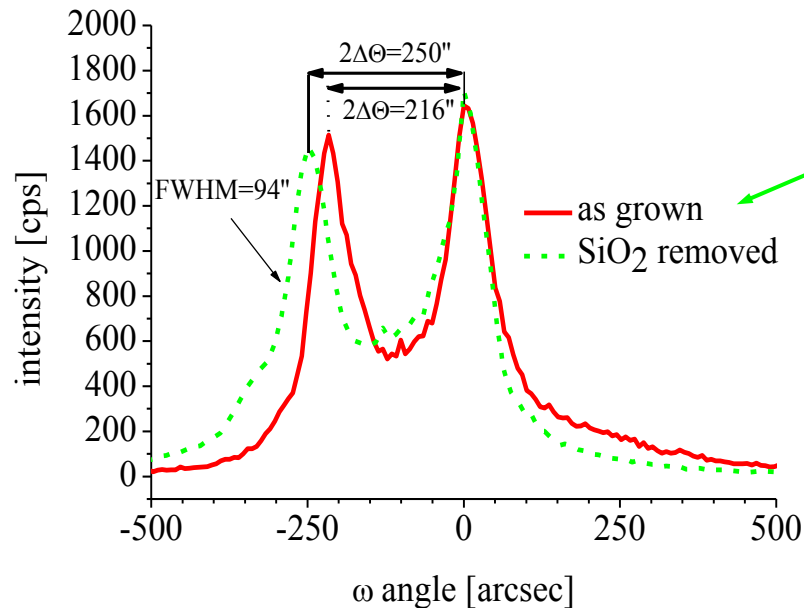
ELO GaAs/Si:

- wings hanging over the SiO₂ mask (no mask-induced tilt)
- wings tilted upwards

GaAs/Si
$\alpha_{\text{GaAs}} > \alpha_{\text{Si}}$
tension in GaAs buffer
upwards tilt

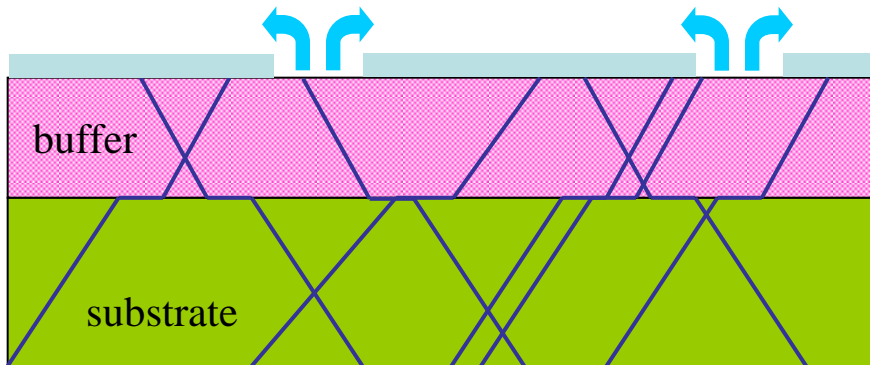
GaN/sapphire
$\alpha_{\text{GaN}} < \alpha_{\text{sapphire}}$
compression in GaN buffer
downwards tilt

Fini et al. Appl. Phys. Lett. 2000

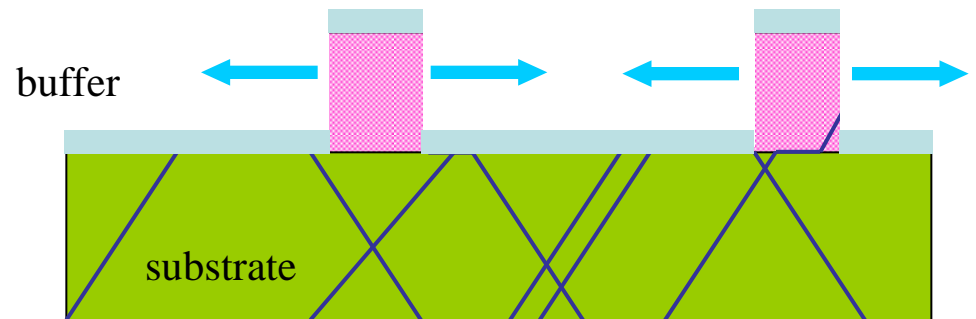


Another ELO concepts (e.g. Pendeo-epitaxy)

Epitaxial Lateral Overgrowth



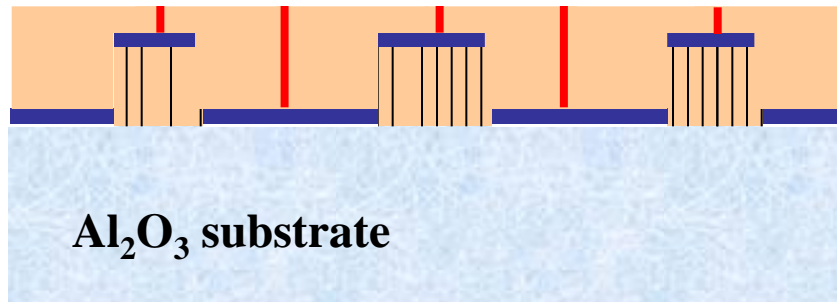
New concept



Pendeo-epitaxy

pendeo - “hanging on”
 “suspending from”

™ Nitronex Corp., Raleigh,
 North Caroline University

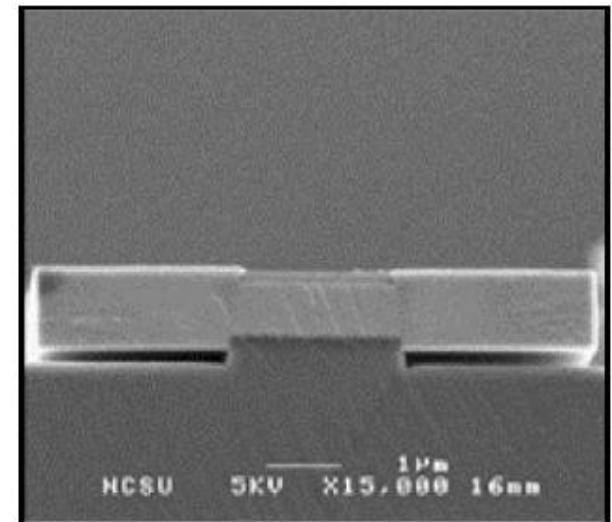


PE GaN

GaN buffer

mask

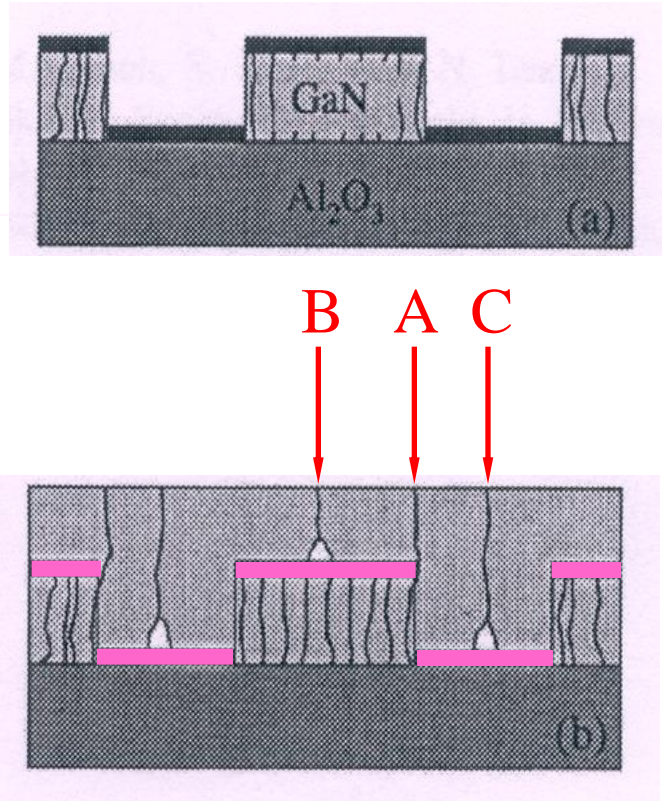
Davis et al. JCG 2001



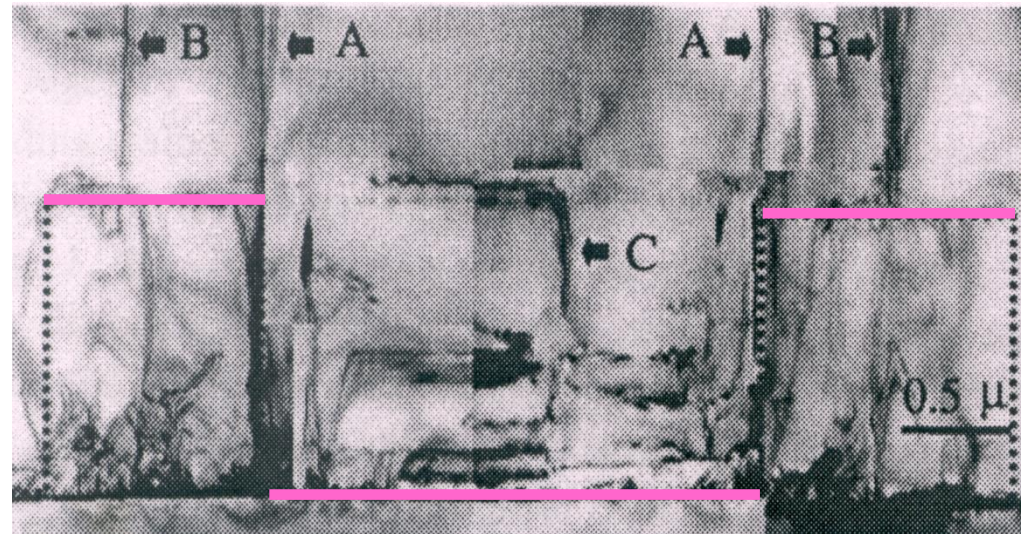
**PE vs. ELO: reduction of TD density over the whole wafer
 within one PE process**

Pendeo-epitaxy

Chen et al. APL 1999



TEM

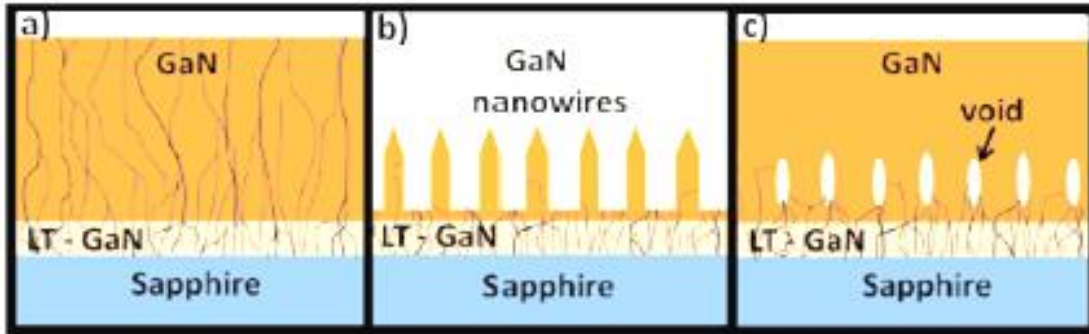


Advantage: maskless versions of PE possible for GaN on SiC or SiC-coated Si

Strittmatter et al. APL 2001; Davis et al. JCG 2001

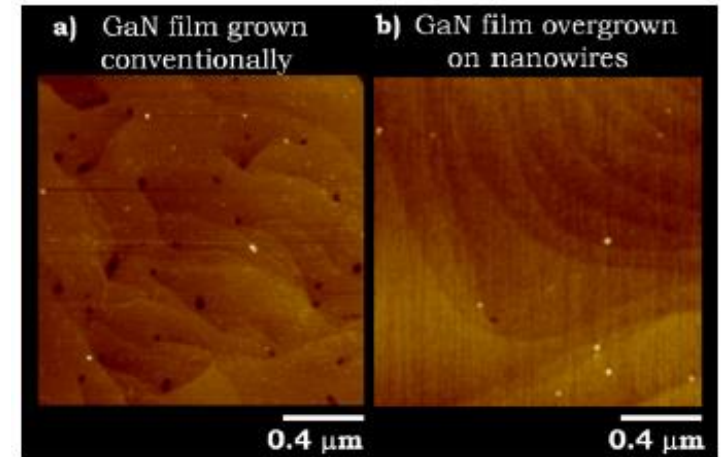
EVA – Embedded Void Approach

Frajtag et al. APL 2011 98 023115

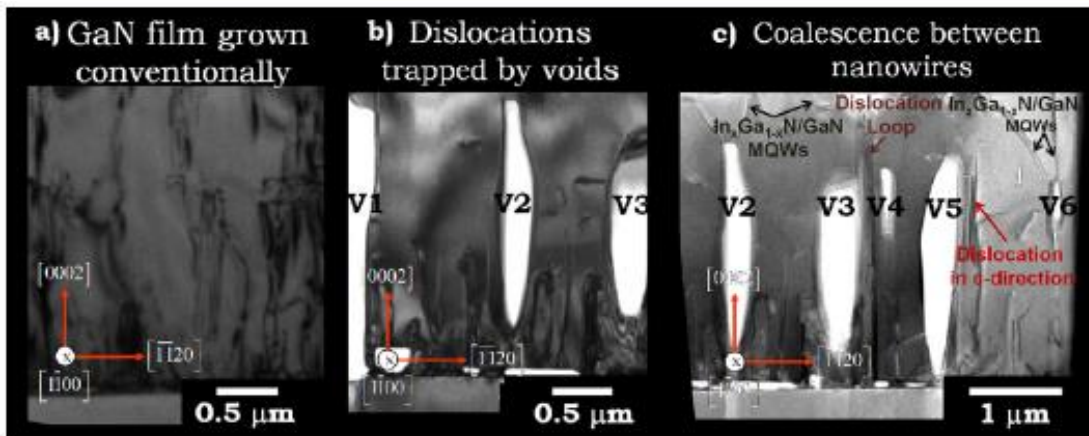


$2.1 \times 10^9 \text{ cm}^{-2}$

$3.9 \times 10^7 \text{ cm}^{-2}$

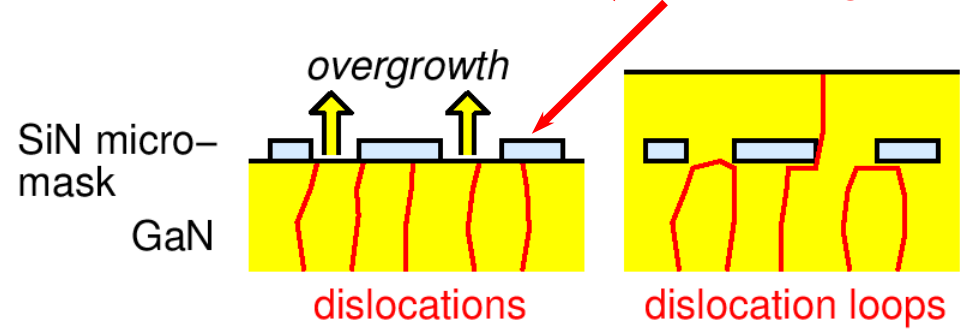


AFM



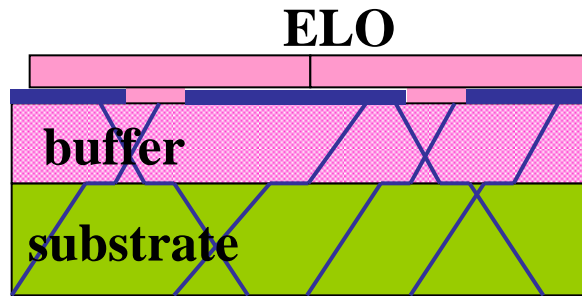
TEM

“random” mask (SiN coverage below 1 ML)



S. Tanaka et al., Jpn. J. Appl. Phys. 39, L831 (2000)

ELO summary



a tool for fabrication of low-dislocation density epilayers on heavily dislocated substrates

take from the seed info on crystal lattice; do not take defects!!!

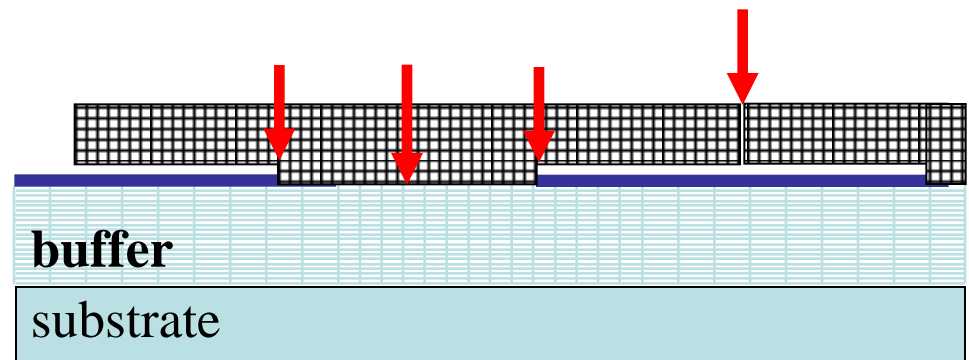
ELO – all lattice mismatch-induced problems solved?

Achievements:

1. significant reduction of dislocation density in lattice-mismatched heterostructures
2. easier elastic relaxation of thermal strain

Problems:

1. interaction of ELO layers with the mask; bending
2. generation of defects at the front of coalescence



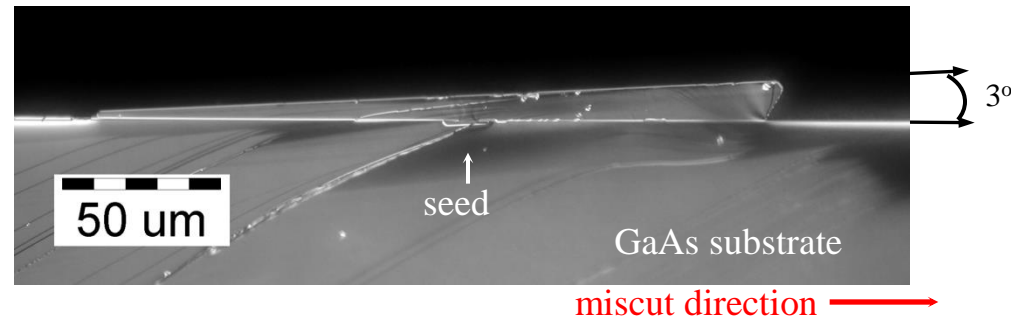
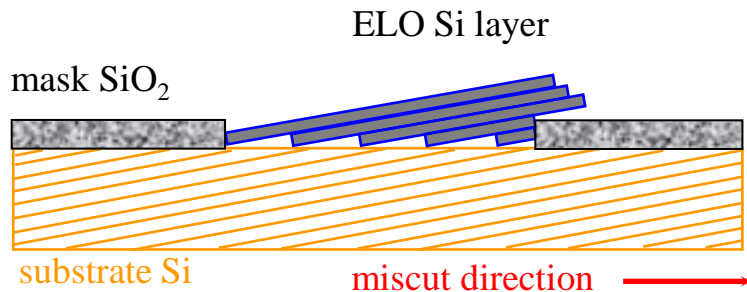
Mechanism of ELO growth on dislocated substrates

comparison

ELO on dislocation-free substrate
Si/Si

ELO on dislocated substrate
GaAs/GaAs

Zytkiewicz et al. Cryst. Res. Technol. 2005



growth in the miscut direction only
(for low supersaturation)

growth in all directions

on dislocated substrate ELO growth possible w/o substrate miscut
(miscut used sometimes though; e.g GaAs/Si)

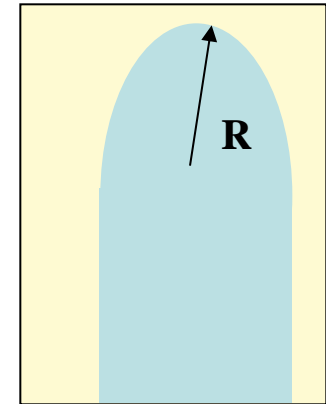
Gibbs-Thomson effect \Rightarrow S. Krukowski's lecture

Gibbs – Thomson effect a – phase equilibrium on curved surface depends on radius of phase boundary

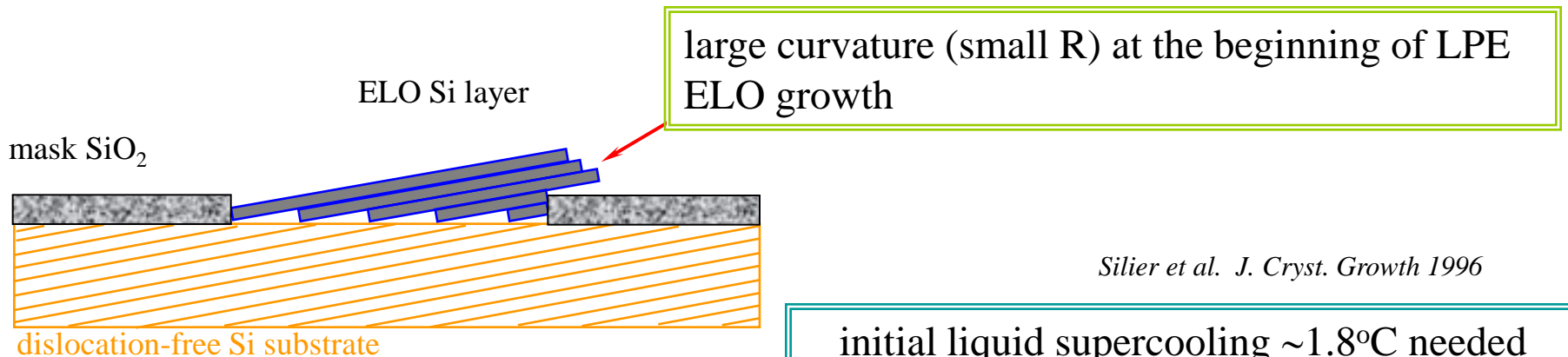
Γ - capillarity constant ($\sim 10^{-7}$ cm = 1 nm)

$$p(R) = p(\infty) \cdot \left(1 + \frac{\Gamma}{R}\right)$$

$$C(R) = C(\infty) \cdot \left(1 + \frac{\Gamma}{R}\right)$$



equilibrium pressure (solute concentration) on curved surface is larger than on the planar one



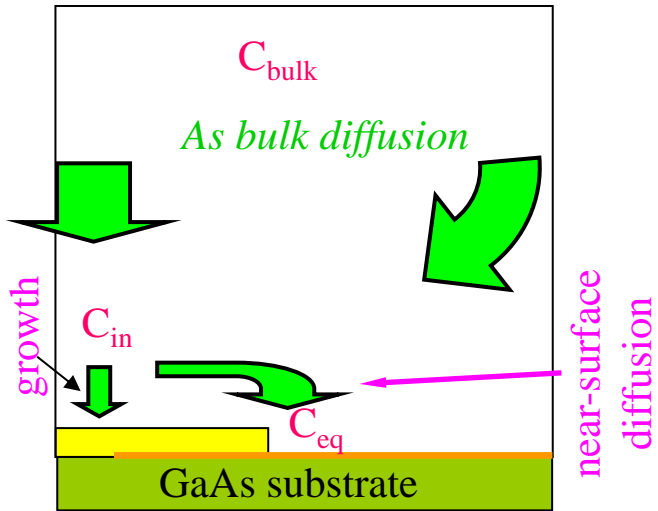
large curvature (small R) at the beginning of LPE ELO growth

Silier et al. J. Cryst. Growth 1996

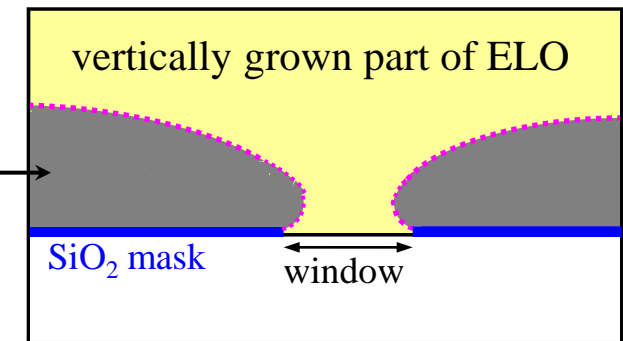
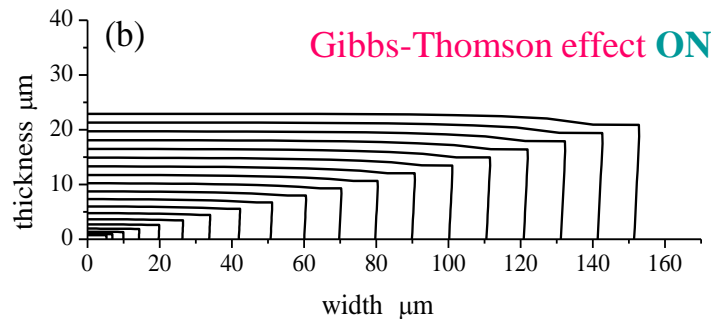
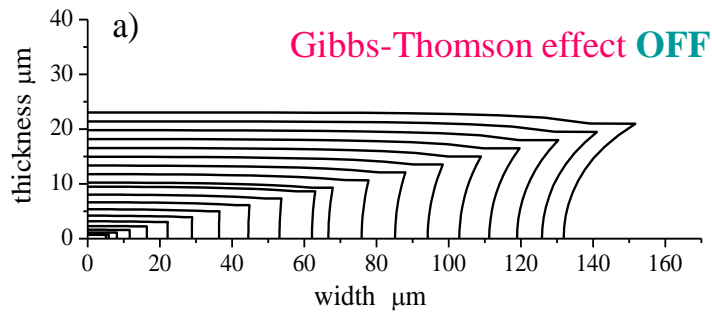
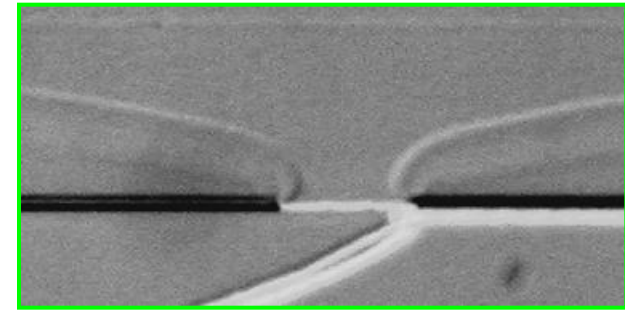
initial liquid supercooling $\sim 1.8^\circ\text{C}$ needed to allow the ELO layer to get out of the channel over the mask

Gibbs-Thomson effect \Rightarrow S. Krukowski's lecture

simulations: ELO of GaAs by LPE



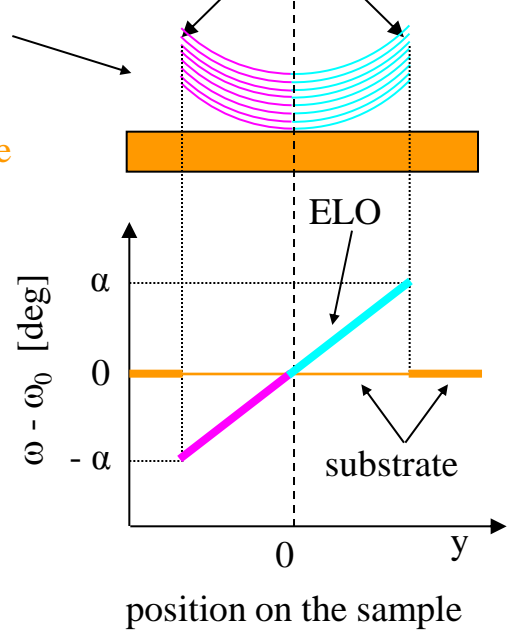
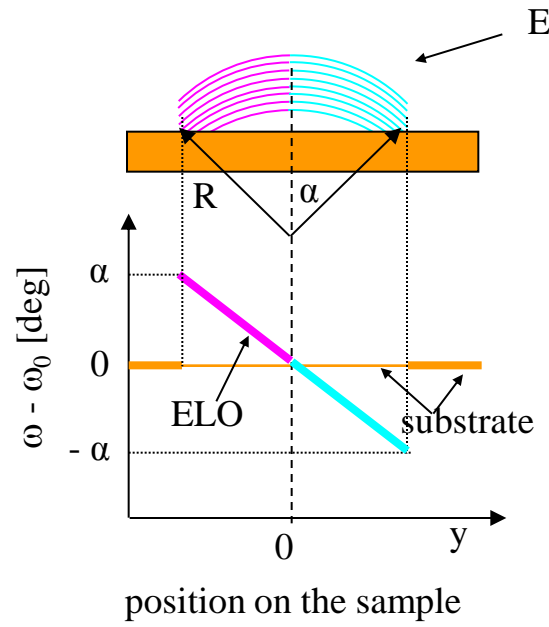
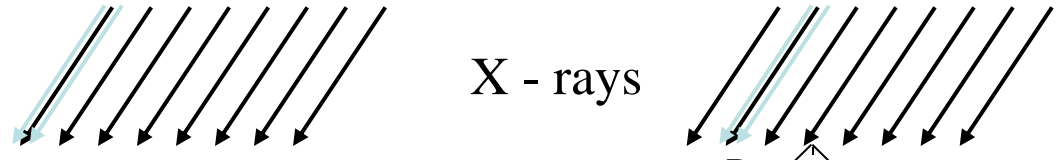
Gibbs-Thomson effect:
ELO of GaAs by LPE



laterally grown part of ELO

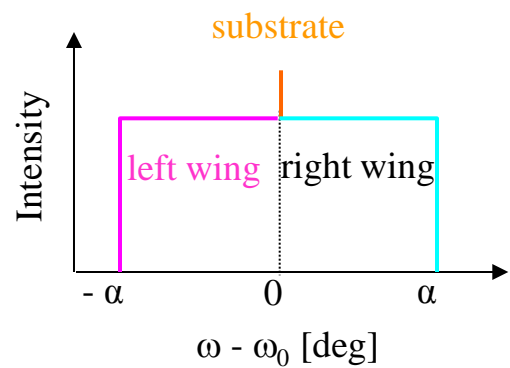
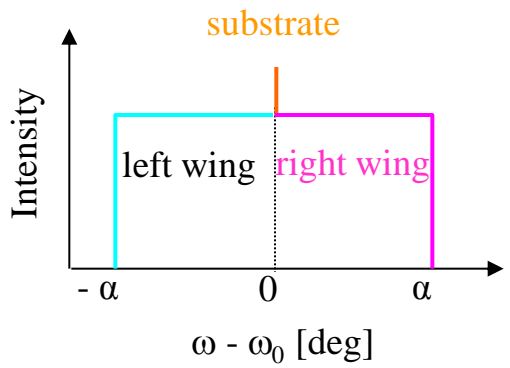
substrate dislocations make ELO growth possible without initial supersaturation of the solution

Lokalna XRD - przykład



SRXRD mapping:

- tilt angle $\alpha(y)$ can be measured
- tilt direction easy to determine
- curvature radius $R(y)$ can be measured locally
- shape of lattice planes can be analyzed $\alpha(y) \sim h'(y)$
- width of ELO can be measured



Standard Rocking Curve:

- tilt angle α can be measured
- tilt direction cannot be determined